Submarine Gas Hydrate Reservoir Simulations – A Gas/Liquid Fluid Flow Model for Gas Hydrate Containing Sediments

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Reservoir model principles

Phases

- 3 solid phases: sediment, methane hydrate, CO_2 hydrate
- 2 fluid phases: gas phase, water (liquid) phase
- (1 supercritical phase: supercritical CO₂ not implemented yet)

Components

- 2 gas phase components: methane, carbon dioxide
- 3 components solved in water: sea salt, methane, carbon dioxide

Pressure equation: advanced 2-phase Darcy model

Energy equation: flow through porous solid, hydrate extensions, latent heats, pressure work



Continuity equations:

$$\begin{array}{l} \displaystyle \frac{\partial}{\partial t} \left(\phi S_{_{G}} \rho_{_{G}} \right) & + \nabla \cdot \left(\rho_{_{G}} \mathbf{u}_{_{G}} \right) = s_{_{G}} \\ \displaystyle \frac{\partial}{\partial t} \left(\phi S_{_{L}} \rho_{_{L}} \right) & + \nabla \cdot \left(\rho_{_{L}} \mathbf{u}_{_{L}} \right) = s_{_{L}} \end{array} \right) & \quad \text{Euler/Euler} \\ \displaystyle \frac{\partial}{\partial t} \left(\phi S_{_{MH}} \rho_{_{MH}} \right) & = s_{_{MH}} \\ \displaystyle \frac{\partial}{\partial t} \left(\phi S_{_{CH}} \rho_{_{CH}} \right) & = s_{_{CH}} \end{array}$$

Saturation:
$$S_{j} = \frac{\varepsilon_{j}}{1 - \varepsilon_{s}} = \frac{\varepsilon_{j}}{\phi} = \frac{\text{volume fraction of phase } j}{\text{sediment free volume fraction}}$$

Convection splitted form:

$$\phi \frac{\partial S}{\partial t} + \phi S \frac{1}{\rho} \frac{\partial \rho}{\partial t} + \nabla \cdot \mathbf{u} + \mathbf{u} \cdot \frac{\nabla \rho}{\rho} = \frac{s}{\rho}$$



Density derivatives:
$$\chi = \frac{1}{\rho} \left(\frac{\partial \rho}{\partial P} \right)_{T, y_k}, \quad \beta = -\frac{1}{\rho} \left(\frac{\partial \rho}{\partial T} \right)_{P, y_k}, \quad \varphi_k = \frac{1}{\rho} \left(\frac{\partial \rho}{\partial y_k} \right)_{P, T}$$

$$\frac{1}{\rho} \frac{\partial \rho}{\partial t} = \chi \frac{\partial P}{\partial t} - \beta \frac{\partial T}{\partial t} + \sum_k \varphi_k \frac{\partial y_k}{\partial t}, \quad \frac{\nabla \rho}{\rho} = \chi \nabla P - \beta \nabla T + \sum_k \varphi_k \nabla y_k$$

General form:

$$\left(\phi \frac{\partial S}{\partial t} \right) + \phi S \left(\chi \frac{\partial P}{\partial t} - \beta \frac{\partial T}{\partial t} + \sum_{k} \varphi_{k} \frac{\partial y_{k}}{\partial t} \right) + \nabla \cdot \mathbf{u} + \mathbf{u} \cdot \left(\chi \nabla P - \beta \nabla T + \sum_{k} \varphi_{k} \nabla y_{k} \right) = \frac{s}{\rho}$$

Darcy equation:

$$\begin{split} \mathbf{u} &= -\mathbf{K}_{\!_{f}} \Lambda \left(\nabla P + \mathbf{g} \rho \right) \quad \text{with} \quad \Lambda = \frac{k_{_{rel}}}{\eta} \,, \quad k_{_{rel}} = f \left(S_{_{H}}, S_{_{L}} \right) \\ &\sum_{_{j}} S_{_{j}} = 1 \,, \left(\sum_{_{j}} \phi \frac{\partial S_{_{j}}}{\partial t} = 0 \right) \end{split}$$

Phase summation:



Insertion in general form and summation over phases leads to general pressure equation:

$$\begin{split} \phi \sum_{j} S_{j} \chi_{j} \frac{\partial P_{j}}{\partial t} + \nabla \cdot \left(-\mathbf{K}_{f} \sum_{j} \Lambda_{j} \left(\nabla P_{j} + \mathbf{g} \rho_{j} \right) \right) \\ - \mathbf{K}_{f} \sum_{j} \Lambda_{j} \left(\chi_{j} \left(\nabla P_{j} + \mathbf{g} \rho_{j} \right) - \beta_{j} \nabla T + \sum_{k} \varphi_{k,j} \nabla y_{k,j} \right) \nabla P_{j} = \\ \sum_{j} \frac{q_{j}}{\rho_{j}} + \phi \sum_{j} S_{j} \left(\beta_{j} \frac{\partial T}{\partial t} - \varphi_{k,j} \frac{\partial y_{k,j}}{\partial t} \right) - \mathbf{K}_{f} \mathbf{g} \sum_{j} \Lambda_{j} \rho_{j} \left(\beta_{j} \nabla T - \sum_{k} \varphi_{k,j} \nabla y_{k,j} \right) \end{split}$$

Capillary pressure: $P_{_{C}} = P_{_{G}} - P_{_{L}}$ with $P_{_{C}} = f(S_{_{H}}, S_{_{L}})$

Calculation pressure:

$$P = \frac{1}{2} \Big(P_{\scriptscriptstyle L} + P_{\scriptscriptstyle G} \Big) \quad \rightarrow \quad P_{\scriptscriptstyle L} = P - \frac{1}{2} P_{\scriptscriptstyle C} \ , \quad P_{\scriptscriptstyle G} = P + \frac{1}{2} P_{\scriptscriptstyle C}$$





Reservoir Model – Energy Equations

Summation over single phase energy equations with $T_{_G} = T_{_L} = T_{_H} = T_{_S}$

$$\begin{split} \phi S_{G}\rho_{G}c_{P,G}\frac{\partial T_{G}}{\partial t}+\nabla\cdot\left(-\phi S_{G}\boldsymbol{\lambda}_{G}\nabla T_{G}\right)-\mathbf{K}_{f}A_{G}\left(\nabla P_{G}+\mathbf{g}\rho_{G}\right)\rho_{G}c_{P,G}\nabla T_{G}=\dot{q}_{P}\\ \phi S_{L}\rho_{L}c_{P,L}\frac{\partial T_{L}}{\partial t}+\nabla\cdot\left(-\phi S_{L}\boldsymbol{\lambda}_{L}\nabla T_{L}\right)-\left(\mathbf{K}_{f}A_{L}\left(\nabla P_{L}+\mathbf{g}\rho_{L}\right)+\varepsilon\nabla S_{L}\right)\rho_{L}c_{P,L}\nabla T_{L}=\dot{q}_{L}\\ \phi\left(S_{MH}\rho_{MH}c_{P,MH}+S_{CH}\rho_{CH}c_{P,CH}\right)\frac{\partial T_{H}}{\partial t}-\nabla\cdot\left(\phi\left(S_{MH}\boldsymbol{\lambda}_{MH}+S_{CH}\boldsymbol{\lambda}_{CH}\right)\nabla T_{H}\right)=\dot{q}_{H}\\ \left(1-\phi\right)\rho_{S}c_{P,S}\frac{\partial T_{S}}{\partial t}+\nabla\cdot\left(-\left(1-\phi\right)\boldsymbol{\lambda}_{S}\nabla T_{S}\right)=0\\ \end{split}$$
Pressure work: $\dot{q}_{P}=\phi S_{G}\beta_{G}T_{G}\frac{\partial P_{G}}{\partial t}+\mathbf{K}_{f}A_{G}\left(\nabla P_{G}+\mathbf{g}\rho_{G}\right)\left(1-\beta_{G}T_{G}\right)\nabla P_{G}$ real gas behaviour Latent heats: $\dot{q}_{H}=-\left(R_{MH}\Delta\tilde{h}_{MH}+R_{CH}\Delta\tilde{h}_{CH}\right)$ (heats of formation)



Reservoir Model – Single Component Equations

Gas phase component, molar fraction conservative form

$$\begin{split} \phi S_{_{G}}\tilde{\rho}_{_{G}}\frac{\partial y_{_{i}}}{\partial t} + y_{_{i}}\frac{\partial}{\partial t}(\phi S_{_{G}}\tilde{\rho}_{_{G}}) + \nabla \cdot \left(-\phi S_{_{G}}\boldsymbol{\delta}^{\text{eff}}_{i,G}\tilde{\rho}_{_{G}}\nabla y_{_{i}} + \mathbf{u}_{_{G}}y_{_{i}}\tilde{\rho}_{_{G}}\right) &= \tilde{q}_{_{i,G}}\\ \frac{\partial}{\partial t}(\phi S_{_{G}}\tilde{\rho}_{_{G}}) &= \phi S_{_{G}}\tilde{\rho}_{_{G}}\left(\frac{1}{S_{_{G}}}\frac{\partial S_{_{G}}}{\partial t} + \chi\frac{\partial P_{_{G}}}{\partial t} - \beta\frac{\partial T}{\partial t} + \sum_{k=1}^{n-1} \left(\varphi_{_{k}} - \frac{\tilde{M}_{_{k}}}{\tilde{M}_{_{G}}}\right)\frac{\partial y_{_{k}}}{\partial t}\right) \end{split}$$

Liquid phase component, molar concentration conservative form

$$\phi S_{_{L}}\frac{\partial c_{_{i,L}}}{\partial t} + c_{_{i,L}}\phi\frac{\partial S_{_{L}}}{\partial t} + \nabla \cdot \left(-\phi S_{_{L}}\boldsymbol{\delta}_{_{i,L}}^{_{e\!f\!f}}\nabla c_{_{i,L}} - \left(\mathbf{K}_{_{f}}\boldsymbol{\Lambda}_{_{L}}\left(\nabla P_{_{L}} + \mathbf{g}\boldsymbol{\rho}_{_{L}}\right) + \boldsymbol{\varepsilon}\nabla S_{_{L}}\right)\boldsymbol{c}_{_{i,L}}\right) = \tilde{\boldsymbol{q}}_{_{i,L}}$$



Reservoir Model – Gas Hydrate Equations

Methane and Carbon Dioxide hydrate saturation

$$\begin{split} \phi \frac{\partial S_{_{MH}}}{\partial t} + \phi S_{_{MH}} \left(\chi_{_{MH}} \left(\frac{\partial P_{_{G}}}{\partial t} - \frac{\partial P_{_{C}}}{\partial t} \right) - \beta_{_{MH}} \frac{\partial T}{\partial t} \right) &= \frac{s_{_{MH}}}{\rho_{_{MH}}} \\ \phi \frac{\partial S_{_{CH}}}{\partial t} + \phi S_{_{CH}} \left(\chi_{_{CH}} \left(\frac{\partial P_{_{G}}}{\partial t} - \frac{\partial P_{_{C}}}{\partial t} \right) - \beta_{_{CH}} \frac{\partial T}{\partial t} \right) &= \frac{q_{_{CH}}}{\rho_{_{CH}}} \end{split}$$

Hydrate kinetics (linearized partial pressure kinetic)

$$\begin{split} R_{_{MH}} &= \frac{1}{V} \frac{\partial N_{_{MH}}}{\partial t} = k_{_{MH}} a_{_{MH}} \left(y_{_M} P_{_G} - P_{_{MH}}^* \right) \\ R_{_{CH}} &= \frac{1}{V} \frac{\partial N_{_{CH}}}{\partial t} = k_{_{CH}} a_{_{CH}} \left(y_{_C} P_{_G} - P_{_{CH}}^* \right) \end{split}$$



COMSOL Implementation

COMSOL Multiphysics implementation essentials

- 3D and 2D axisymmetric models
- Coefficient Form PDE + Heat Transfer in Porous Media
- Discretization/Stabilization as default
- Fully Coupled solution, Direct linear solver (PARDISO)
- Pressure Dirichlet boundary condition given as Weak Constraint
- Initial time step 10 s, maximum time step $5 \cdot 10^6$ s
- maximum mesh size = 15 m, fine meshing at the well



Methods for gas hydrate decomposition





Field production plan





Case Study I – Methane production by Depressurization $P_0 = 92$ bar $T_0 = 10,0^{\circ}C$ $S_{h0} = 0,40$ $H_{res} = 20$ m





Case Study I – Methane production by Depressurization

Methane Production Rate [Nm³/h]





Case Study II – Depressurization of Multi-Layer Reservoir







Case Study II – Depressurization of Multi-Layer Reservoir

Time=3.206278e8 Hydrate Saturation (1)





Case Study II – Depressurization of Multi-Layer Reservoir





SUGAR project – case studies

More case studies developed with COMSOL:

- Injection of Carbon Dioxide with parallel Methane production (2 wells)
- Reservoir simulations for the Ulleung Basin, South Korea (UGBH 2.6)
- Simulation cases for process safety and reservoir integrity issures
- Production upriser pipe simulations (1D / 2Ph Euler Equations)



Summary

State

- Development of a gas hydrate reservoir model in COMSOL Multiphysics
- Usage of the Coefficient Form PDE tool of the Mathematics branch
- Highly nonlinear model, needs the fully coupled approach with direct solution
- Simulation of important reservoir production cases were successful

Outlook

- New 3. project phase starts in October 2014
- Field development simulations in preparation of a real field test
- Production safety simulations



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Thank you for your attention!

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