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# Modeling and Characterization of Superconducting MEMS for Microwave Applications in Radioastronomy

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Project funded by the Rhône-Alpes Region(France)  
IMEP-LAHC(Institute of Microelectronics, Electromagnetism  
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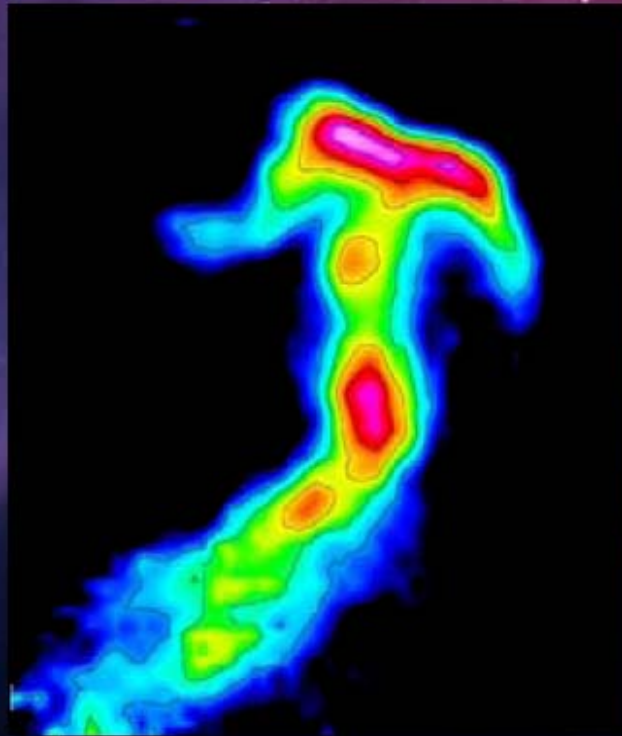
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# Introduction

6/11/2008

Radio-Astronomy Application by IRAM (Institute for Radio-Astronomy Millimetric)



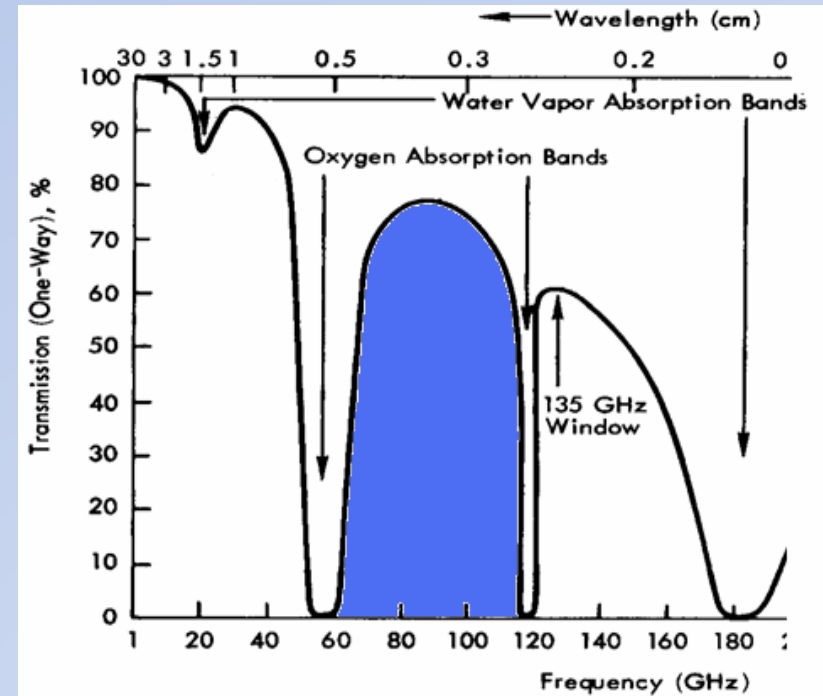
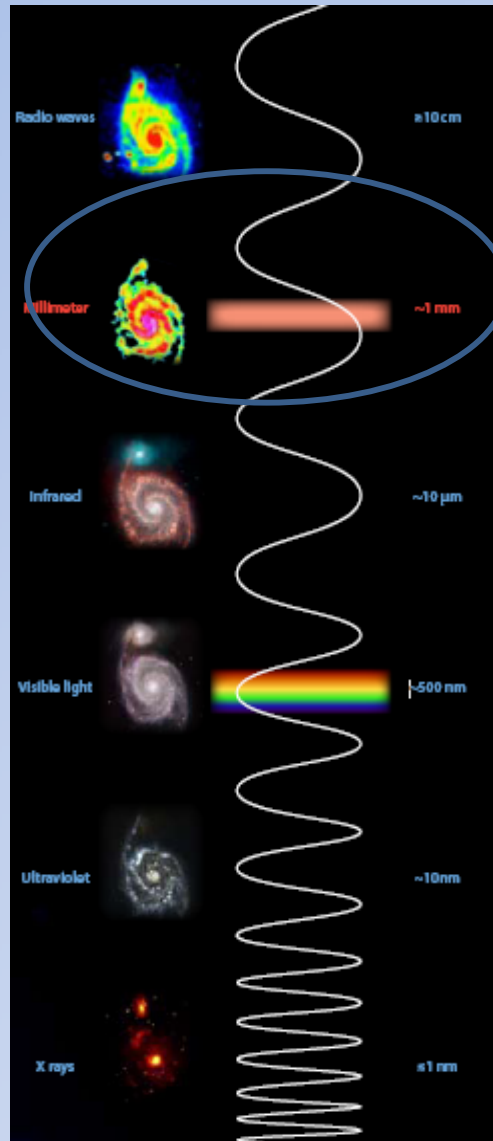
This millimeter image of the famous Horsehead Nebula (named after its optical appearance), which shows the distribution and density of the molecular gas in this dark interstellar cloud, is more reminiscent of a seahorse.



# Introduction

6/11/2008

Radio-Astronomy Application by IRAM (Institute for Radio-Astronomy Millimetric)



## Interstellar molecules

Many molecules were first detected in interstellar clouds, such as the famous Horsehead Nebula.

Rotating on their axis, molecules emit at millimeter wavelengths, each of them with their own characteristic frequencies.

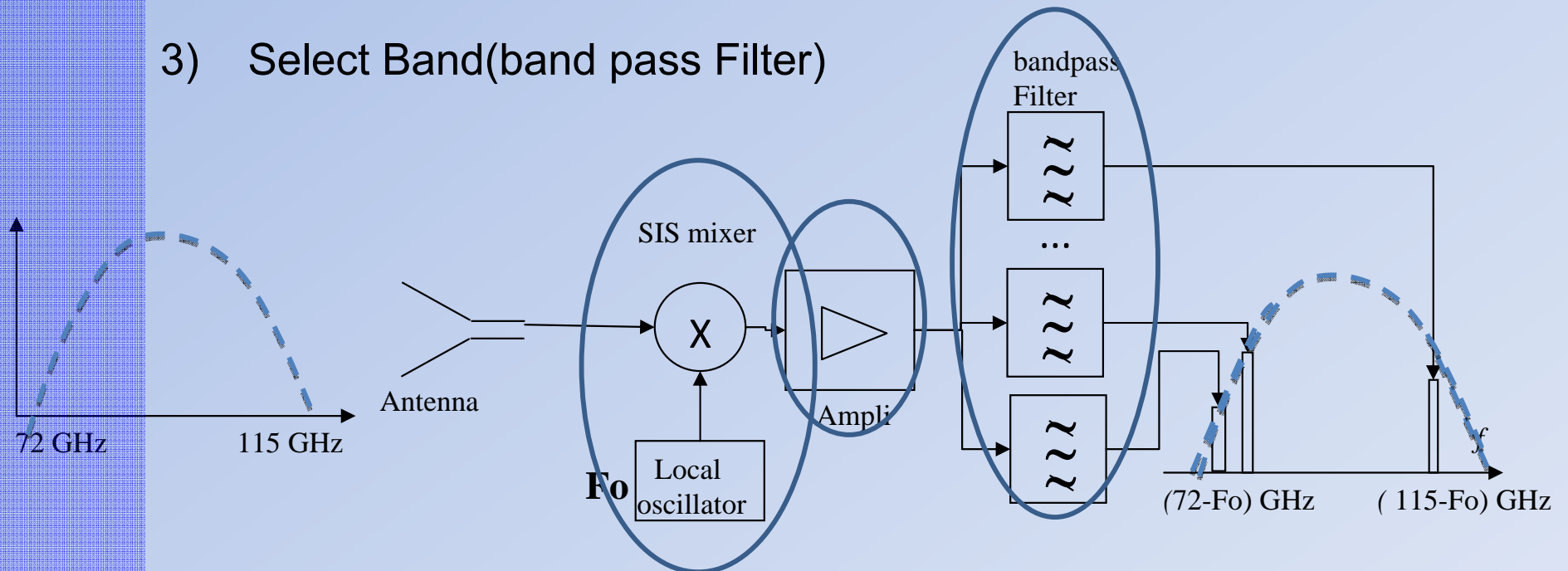
The IRAM telescopes operate at wavelengths of 3, 2, 1 and 0.8 millimeters, the four atmospheric windows where the millimeter emission from space reaches the earth.



# Introduction

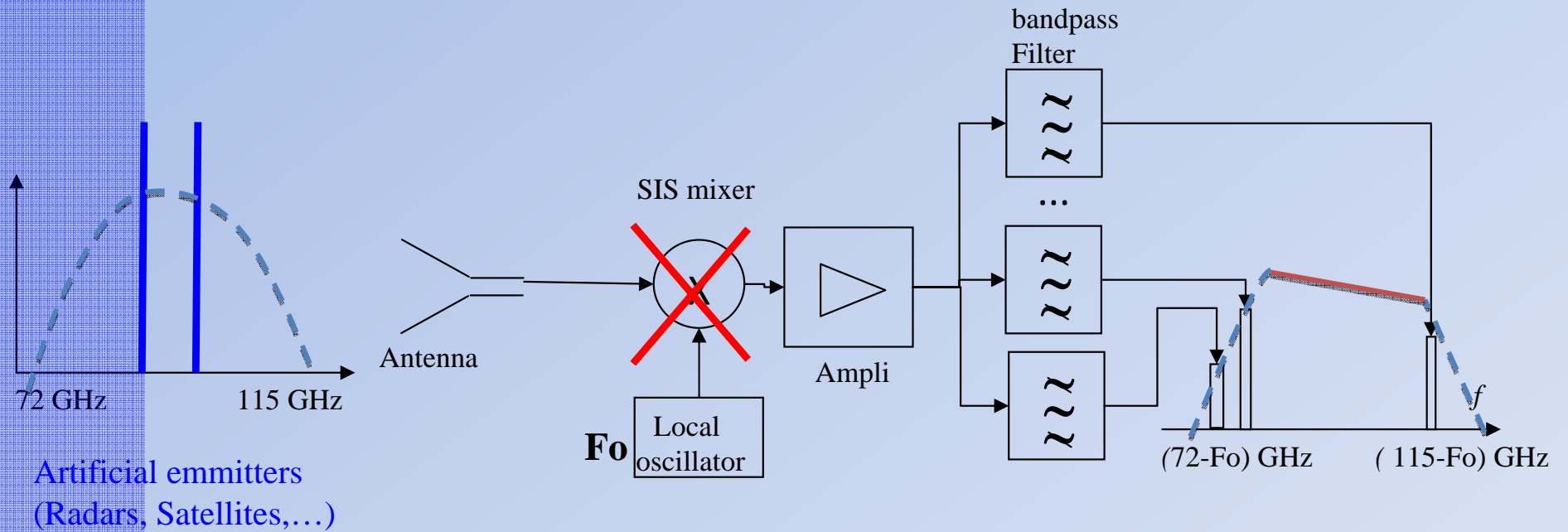
## Heterodyne Receiver Array (HERA)

- 1) signals from cosmic sources are extremely weak ( amplifier)
- 2) Impossible to amplify directly the signals so the frequency of the signal must be lowered (mixer-Local Oscillator)
- 3) Select Band (band pass Filter)



# Introduction

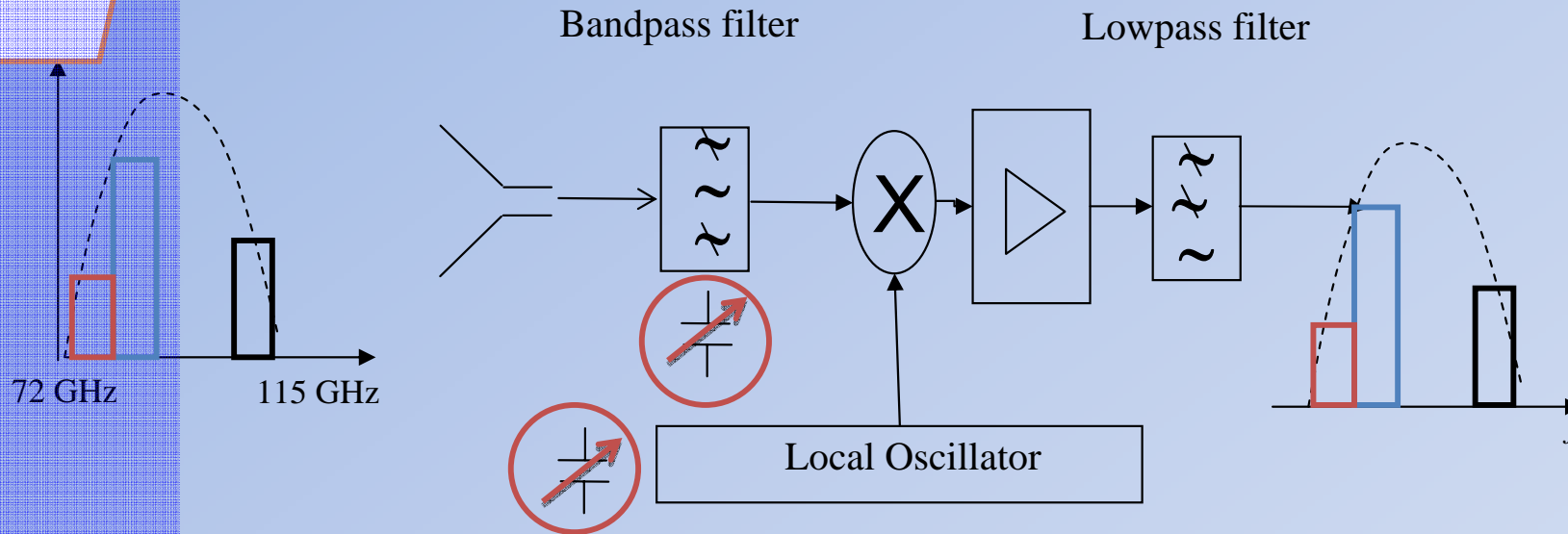
## Heterodyne Receiver Array (HERA)



**Mixer saturation**

# Expected solution

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## 1. Tunability

Solution : integrable tunable capacitor  $\Rightarrow$  MEMS

## 2. Sensitivity

Amplitude is very weak  $\Rightarrow$  Disturbed signal by thermal noise.

Solution : very low temperature superconductor (4 K) « Niobium »



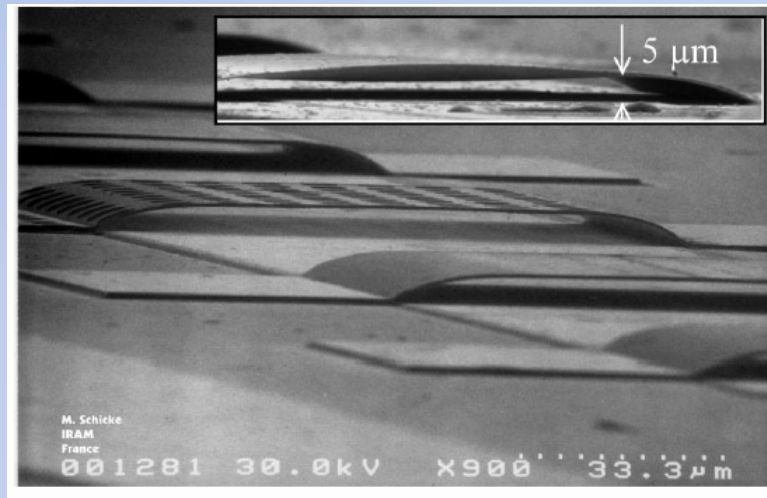
# Multiphysics Modeling

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IRAM Technology  
based on Niobium

Electro-mechanical

Thermics  
(superconducting)



Microwaves



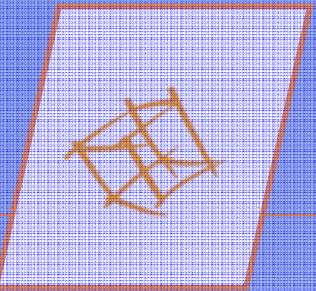
# Outline

6/11/2008

- 1. SupraMems Components**
2. Fabrication process(Experimental observation)
3. Theoretical beam modeling
4. Comsol Multiphysics beam simulation
5. Conclusion and Outlook



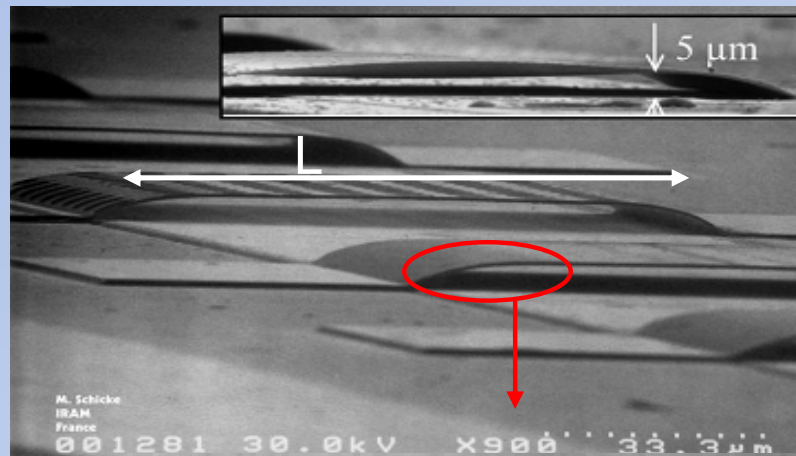




# SupraMems Components?

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- Mems: Micro systems Electro-mechanicals
- Supra: superconducting based on Niobium

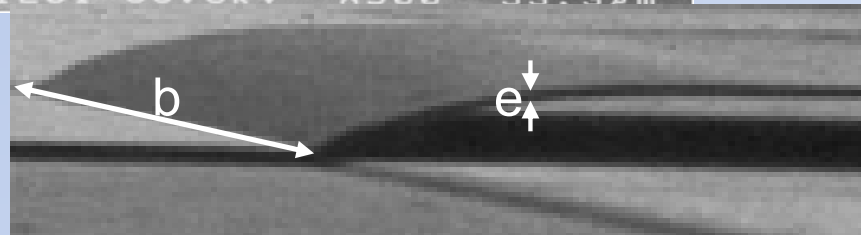


High gap air «g » (4 μm ,5 μm)

length « L » between (60 μm and 90 μm)

Thickness « e » of the beam is (240 nm)

Width « b » is (100 μm)



# Outline

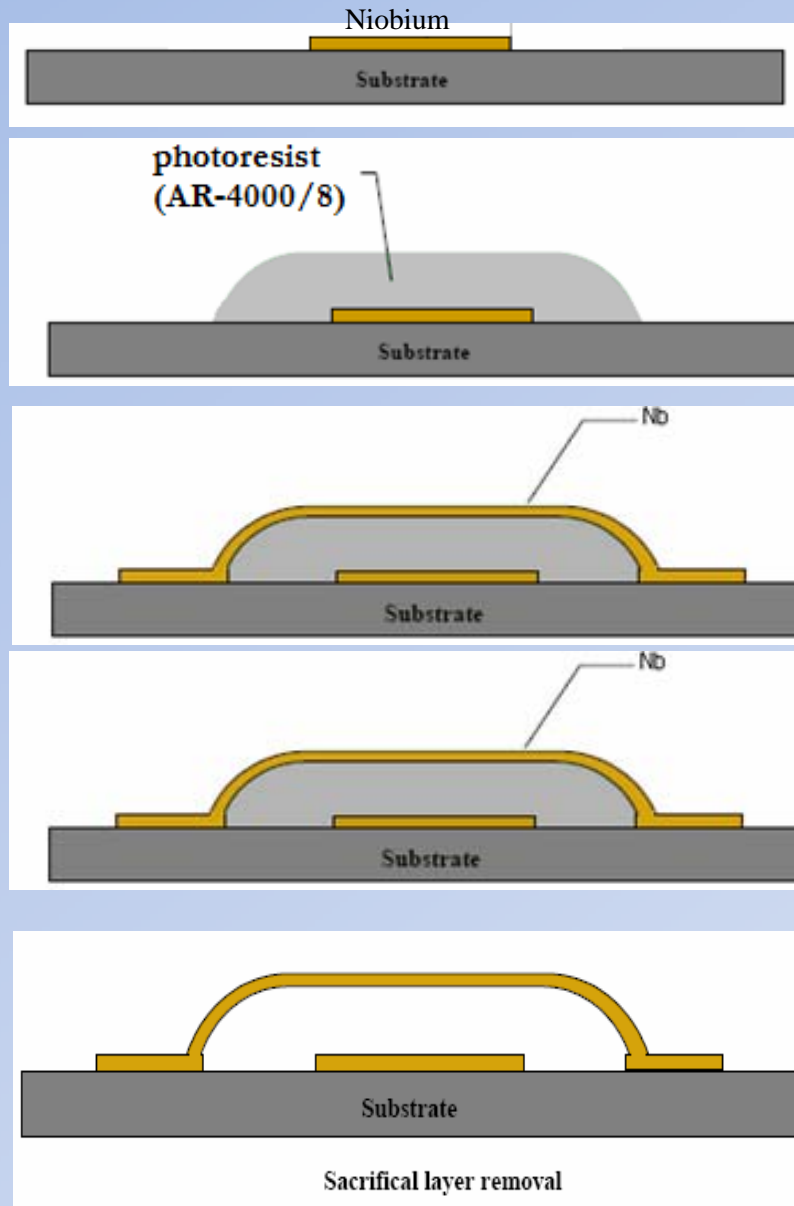
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1. Components Mems
- 2. Fabrication process(Experimental observation)**
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# Fabrication process

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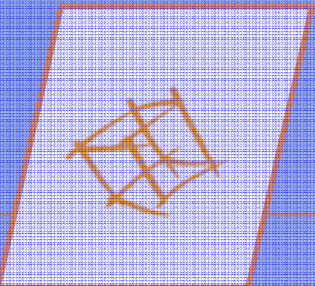
In the first step a Nb contact line is realized

Then, Photoresist polymer AR-4000/8 is used as a sacrificial layer

the Nb layer was sputtered by Dc-magnetron

The widths of the bridges are defined by a photoresist mask and the no-covered parts of the Nb are etched by RIE(Reactive Ion Etching)

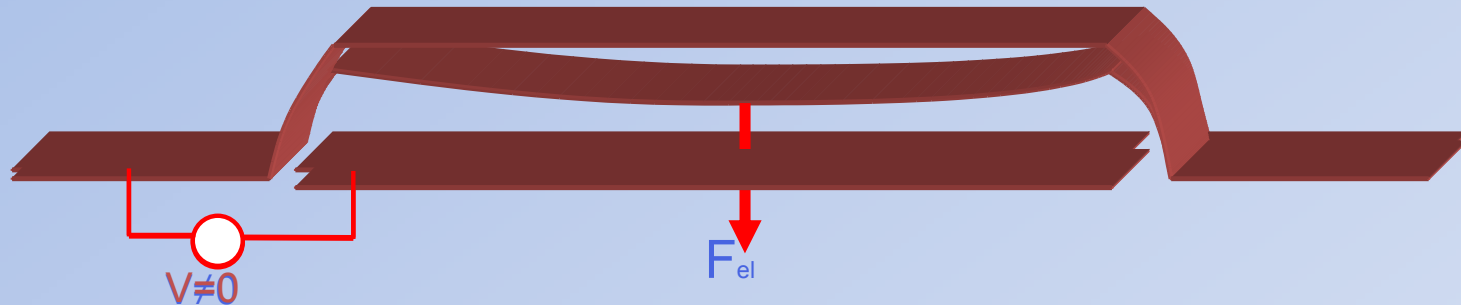
The final step washes away the sacrificial layer in hot acetone



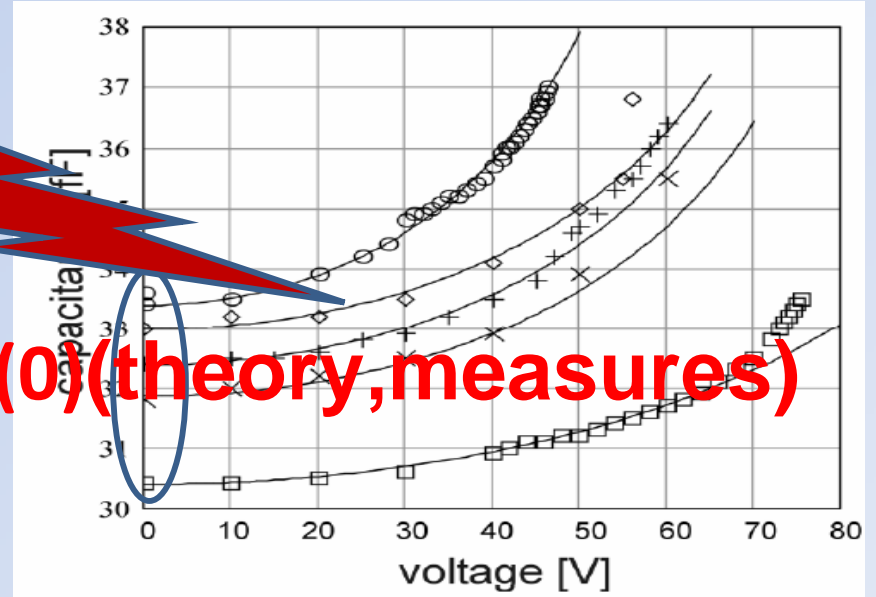
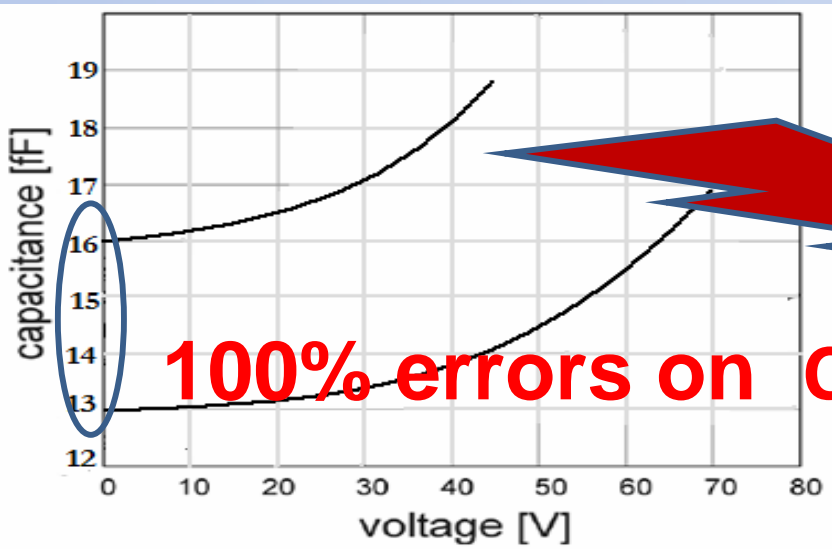
# Experimental observation

6/11/2008

- Varactors capacitances
- Actuated mode is: Electrostatic



- The electrostatic force reduce the air gap "g"
- Expression of capacitor plan:  $C = \frac{\epsilon_0 \times b \times L}{g} \rightarrow C \uparrow$

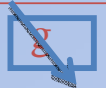


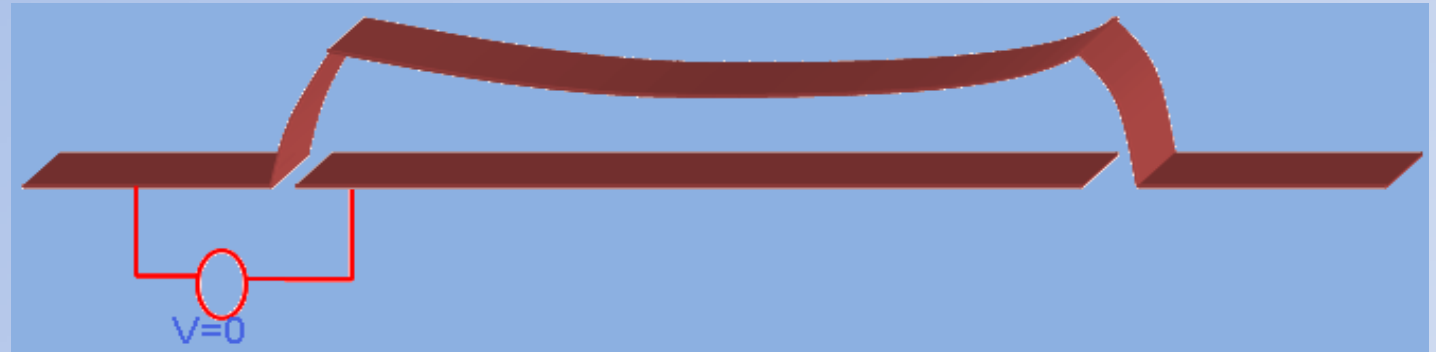
**100% errors on C(0) (theory, measures)**



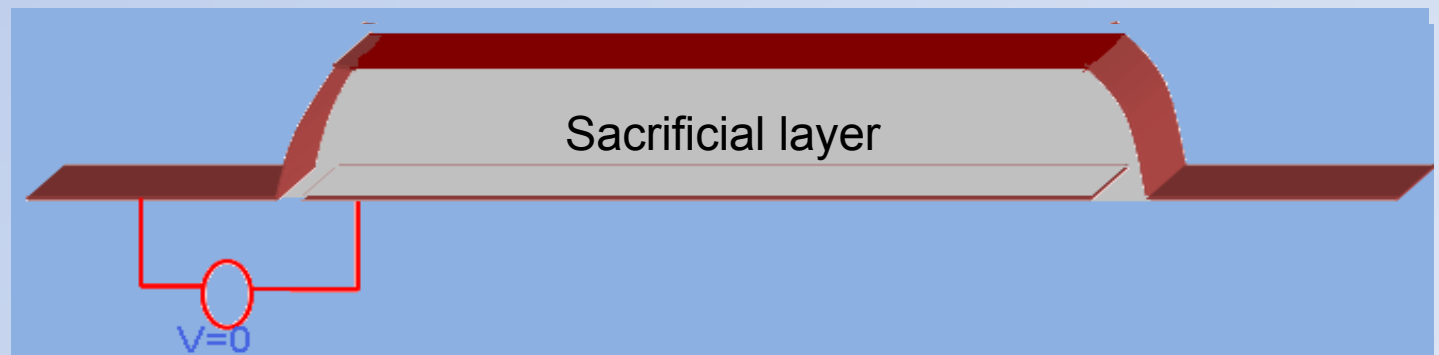
# Experimental observation

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$$C = \frac{\epsilon_0 \times b \times L}{\delta}$$




➤ Lengthening  $\Delta L$  can be caused by a residual tensile stress at the niobium interface which is released when the sacrificial layer is removed

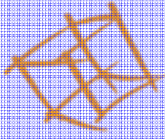


# Outline

6/11/2008

1. Components SupraMemS
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- 3. Theoretical beam modeling**
4. Comsol Multiphysics beam simulation
5. Conclusion and Outlook



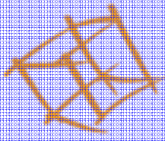


# Theoretical beam modeling

6/11/2008

## Objectives

- Find the values of the capacity  $C(0)$  by determining an equation which describe the profil MEMS
- Determine the expression of  $C(V)$



# Theoretical beam modeling

6/11/2008

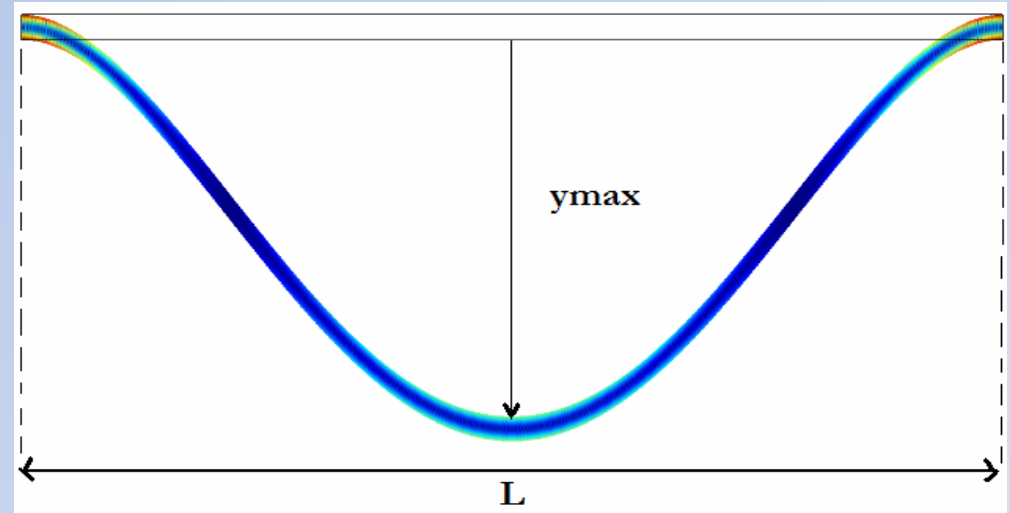
The bending bridge is a Fixed-Fixed beam with a length equal to  $L + \Delta L$ .

Profil en cos

$$y(x) = \frac{y_{\max}}{2} \left( 1 - \cos\left(\frac{2\pi x}{L}\right) \right)$$

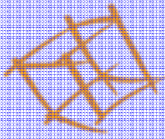
$$C(0) = \int_0^L \frac{\epsilon_0 b}{0g - y(x)} dx$$

$$C(0) = \frac{\epsilon_0 b L}{g \sqrt{1 - \frac{y_{\max}}{g}}}$$



these capacities can be described as the sum of elementary plane capacitance, integration result is.



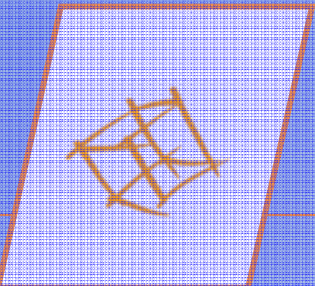


# Theoretical beam modeling

6/11/2008

## Objectives

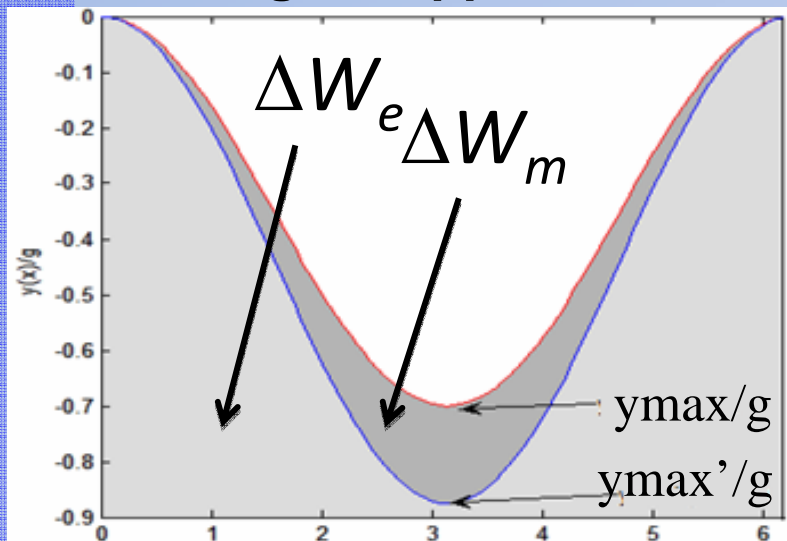
- Find the values of the capacity  $C(0)$  by determining an equation which describe the profil MEMS
- **Determine the expression of  $C(V)$**



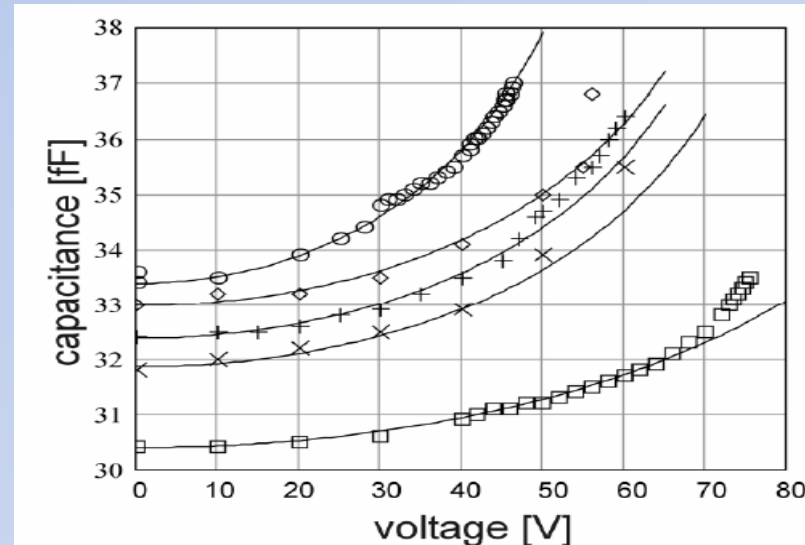
# Theoretical beam modeling

6/11/2008

We assume the same profile on cosines is took when the voltage is applied

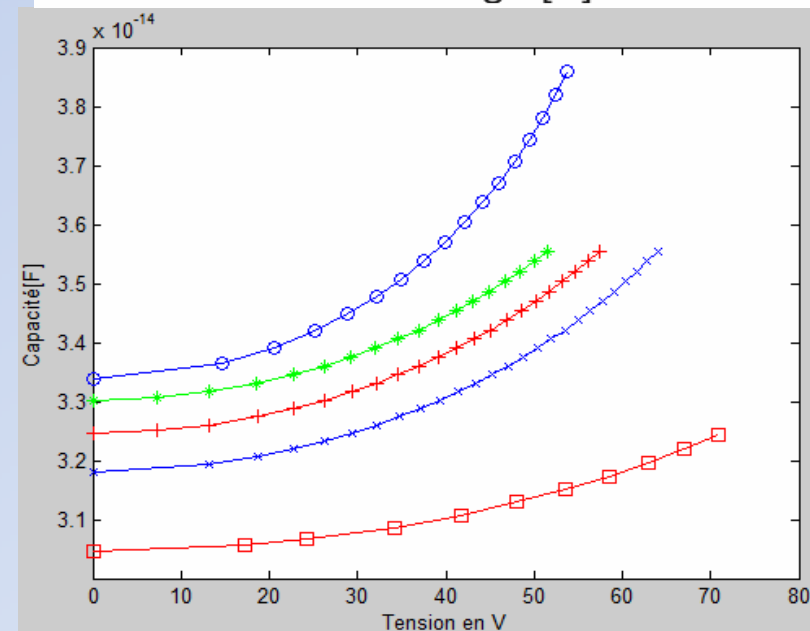


$$W_e = W_m$$



$$V = \sqrt{\frac{g \sqrt{1 - \frac{y_{max}'}{g}} \pi^4 E h y_{max}^2 (y_{max}' - y_{max})^2}{16 L^4 \epsilon_0 W}}$$

$$C = \frac{\epsilon_0 b}{g_0 \sqrt{1 - \frac{y_{max}'}{g_0}}} \quad C(V)$$



# Outline

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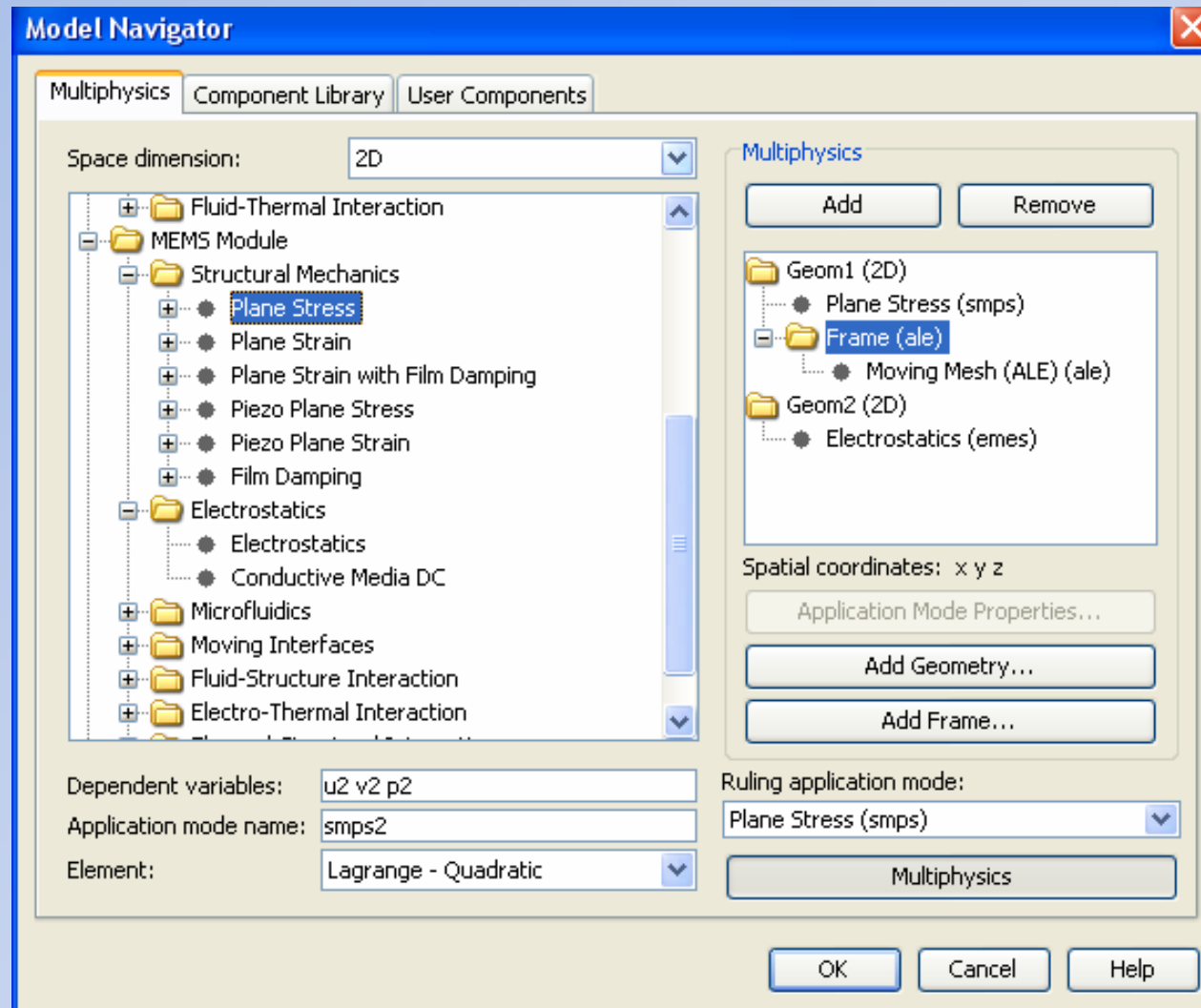
# Comsol Multiphysique beam simulation

## Objectives

- Validate the simple previous theoretical approach (cosinus profile, edge effects neglected) by a multiphysics electromechanical model of the SupraMEMS (COMSOL)
- This approach will be used in future filter designs

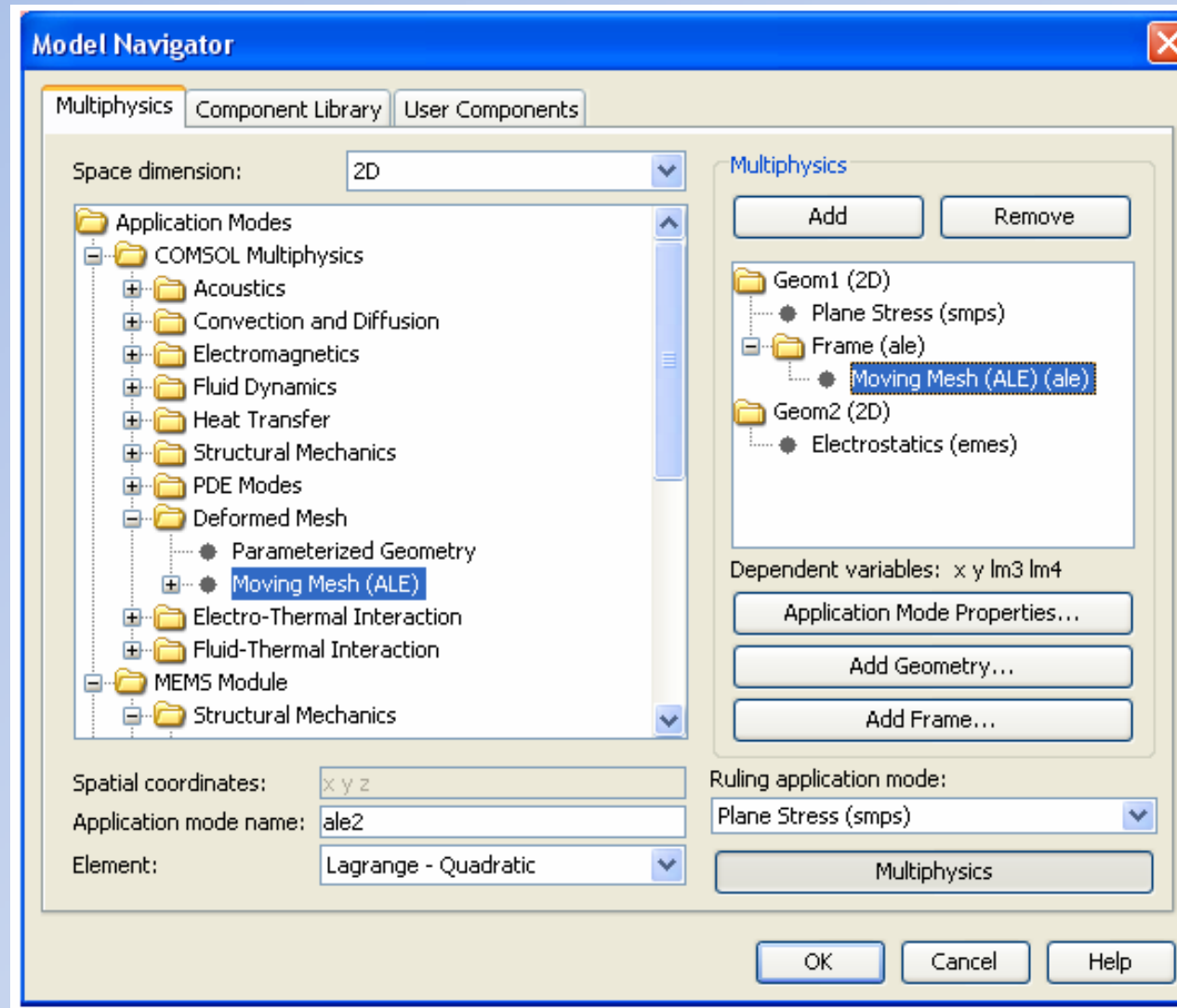
# Comsol Multiphysique beam simulation

Calculate the capacity  $C(0)$

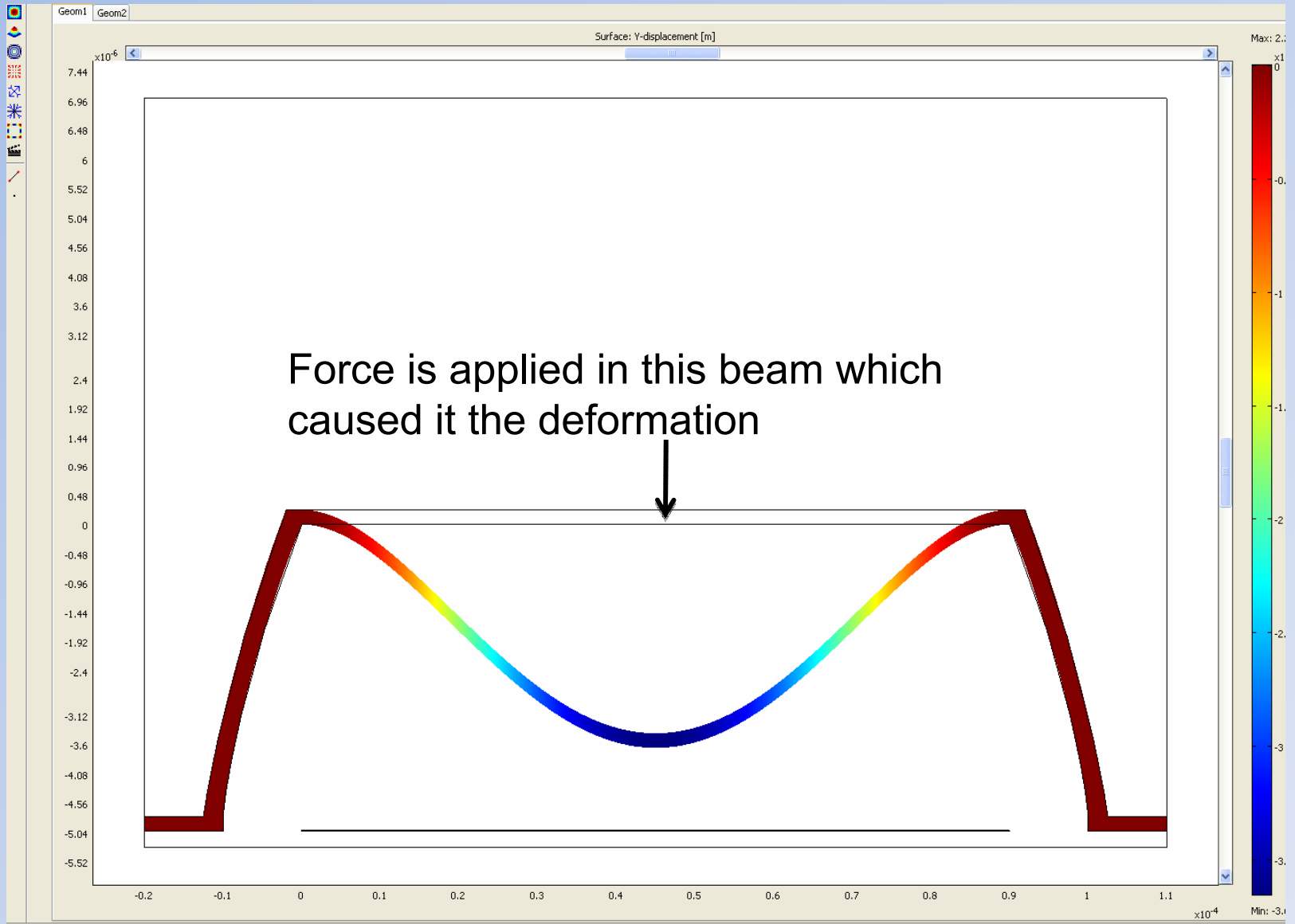


# Comsol Multiphysique beam simulation

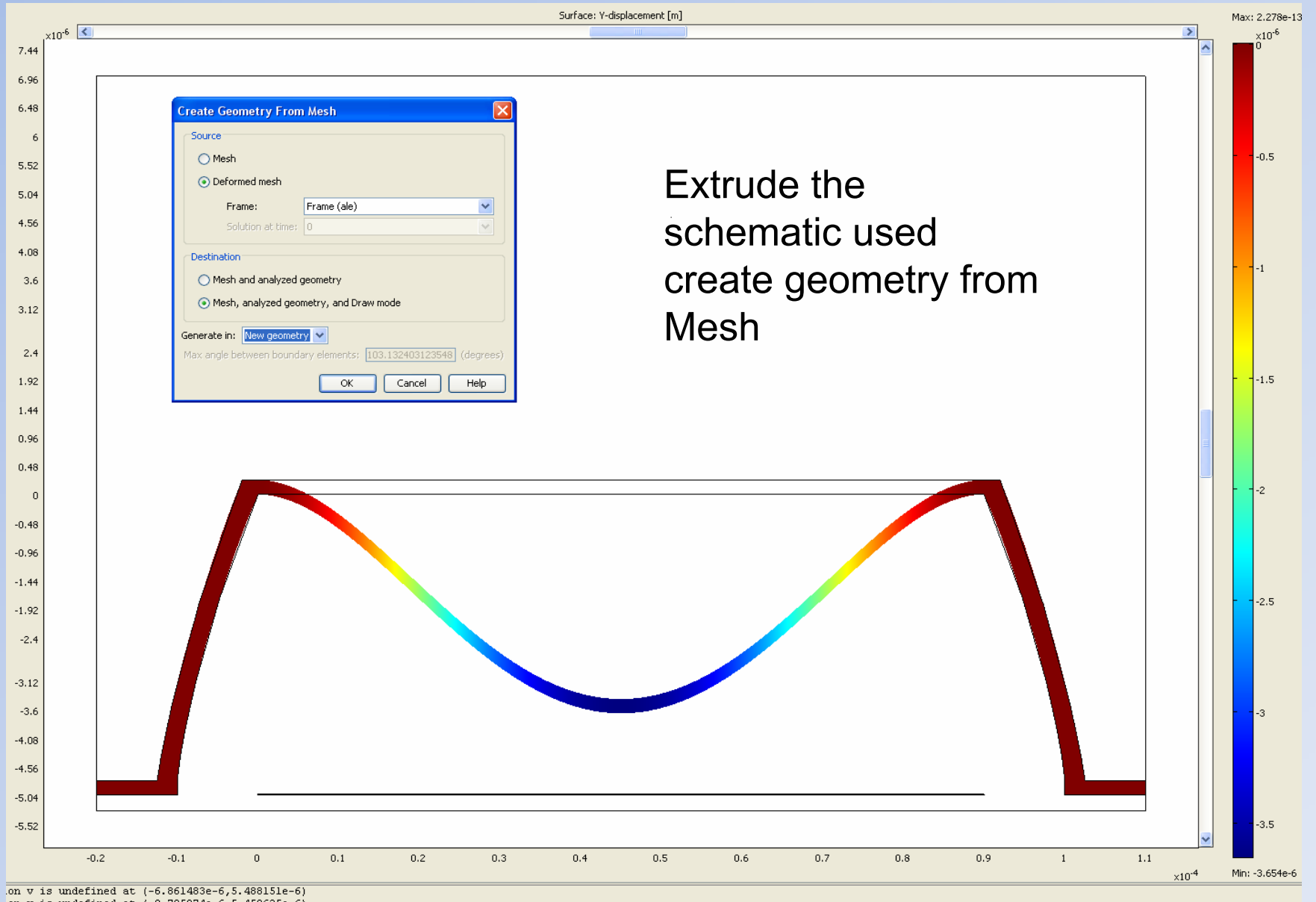
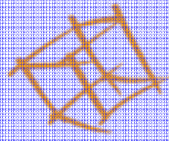
Calculate the capacity  $C(0)$



# Comsol Multiphysique beam simulation



# Comsol Multiphysique beam simulation



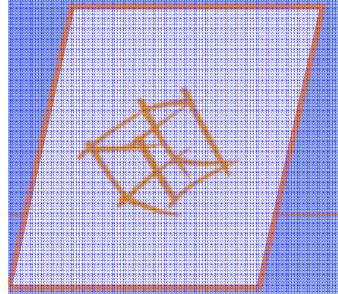
Extrude the schematic used create geometry from Mesh



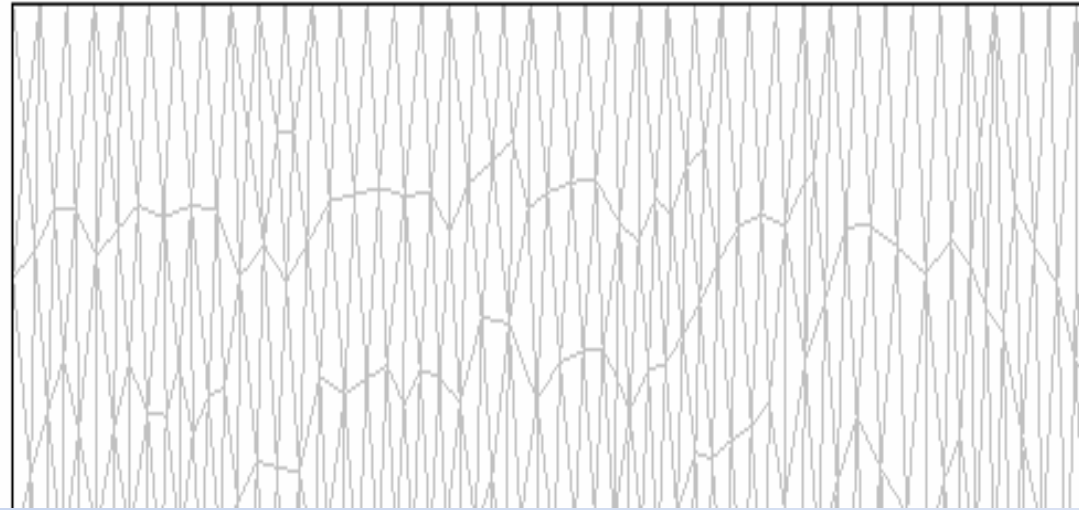
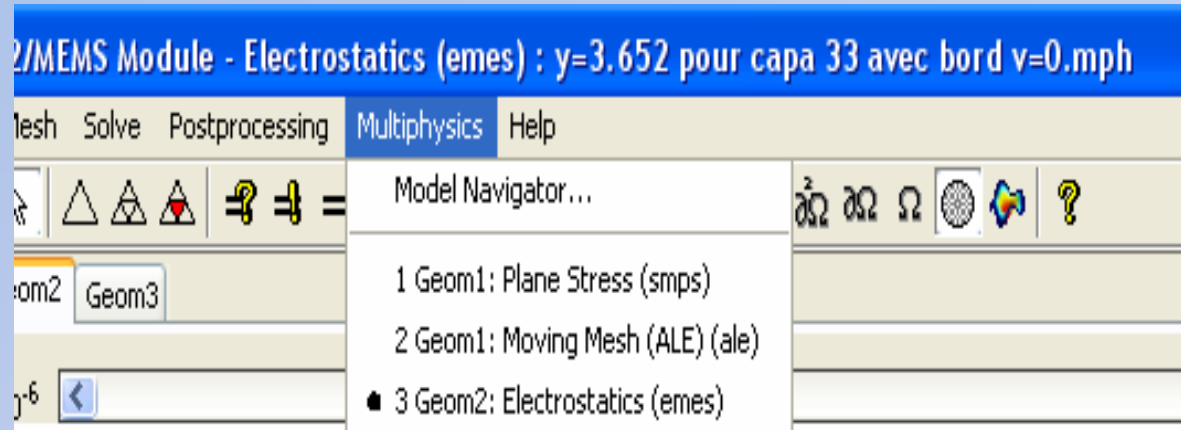
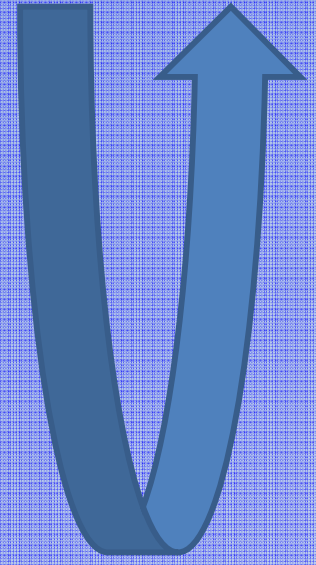
on v is undefined at (-6.861483e-6,5.488151e-6)  
on v is undefined at (-9.795974e-6,5.458625e-6)



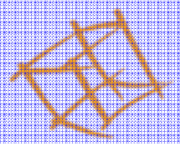
# Comsol Multiphysique beam simulation



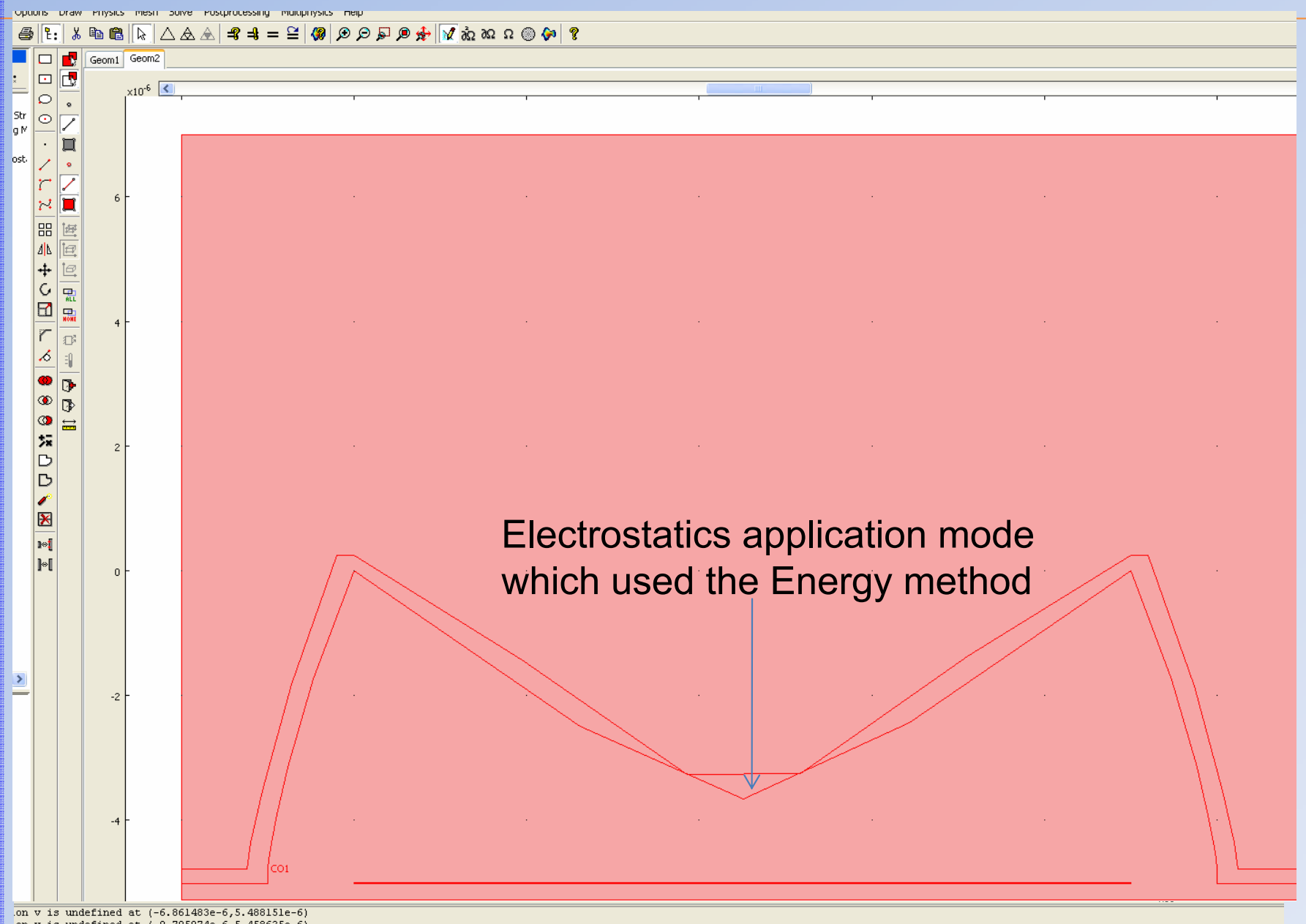
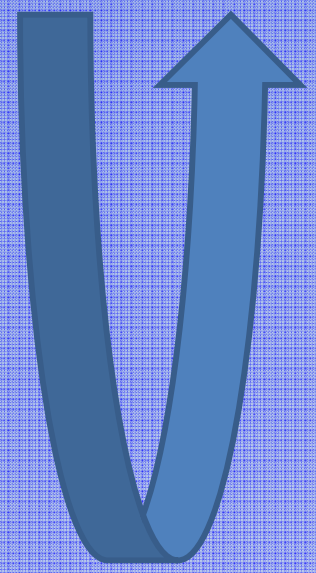
Closed-circuit



# Comsol Multiphysique beam simulation



Closed-circuit

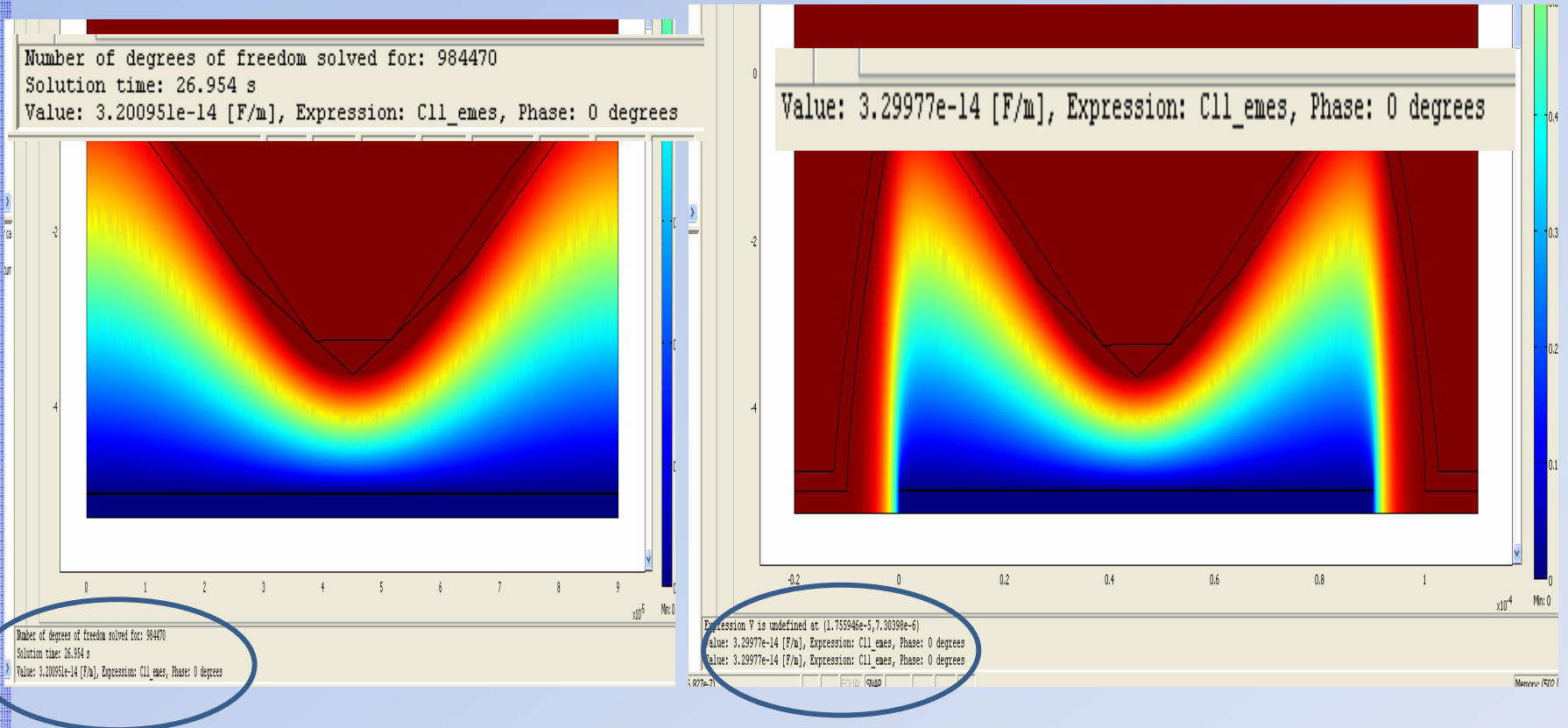


Electrostatics application mode  
which used the Energy method



# Comsol Multiphysique beam simulation

## Surface Electric potentiel



The value of the capacitance is

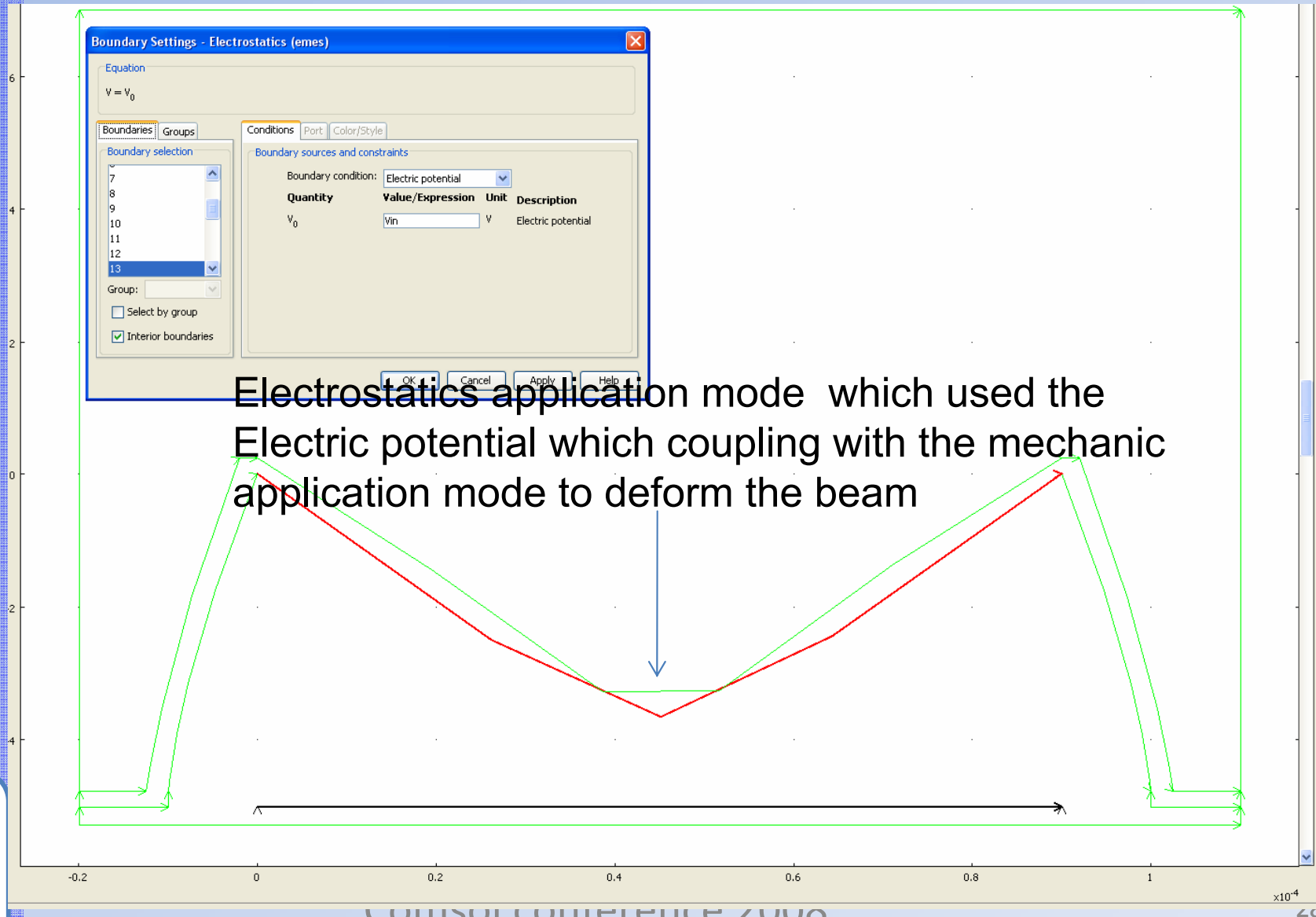
$$C(0) = 2W_e / \Delta V^2 = 32\text{fF}$$

The value of the capacitance is

$$C(0) = 2W_e / \Delta V^2 = 32,99\text{fF}$$

# Comsol Multiphysique beam simulation

Calculate the capacity  $C(V)$

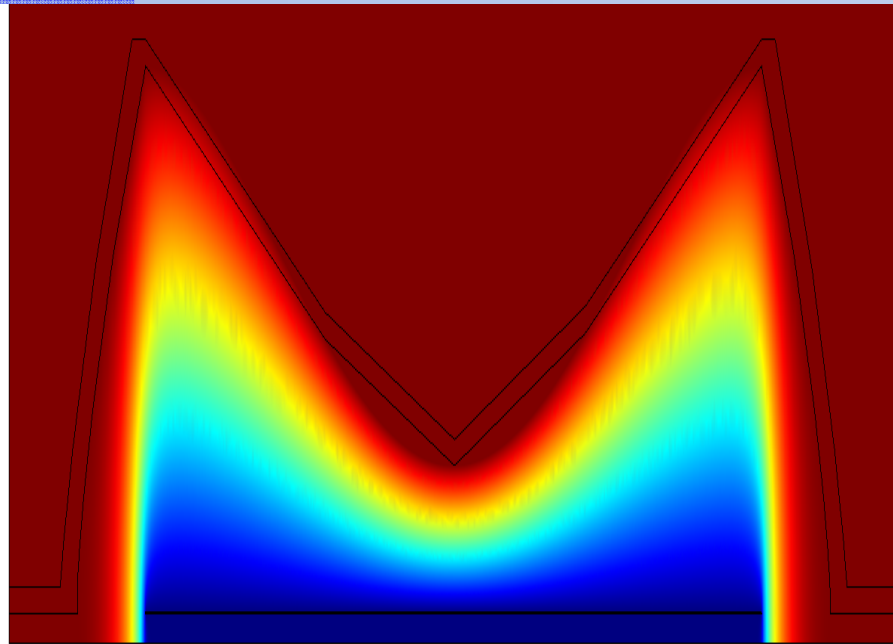


Voltage  $V=45$

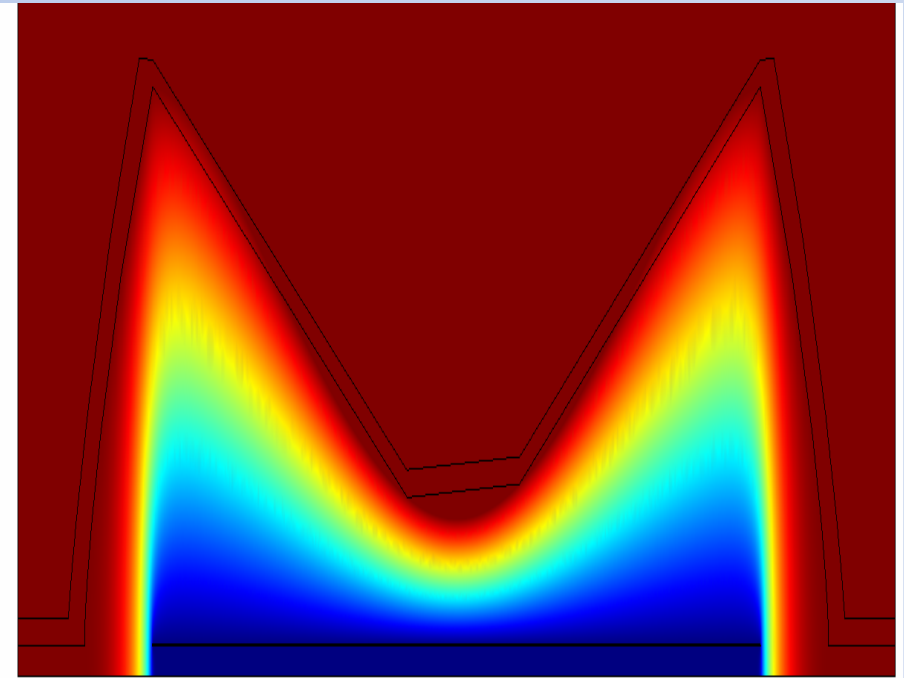
# Comsol Multiphysique beam simulation

Calculate the capacity  $C(V)$

**Surface Electric potentiel**



Voltage  $V=10$



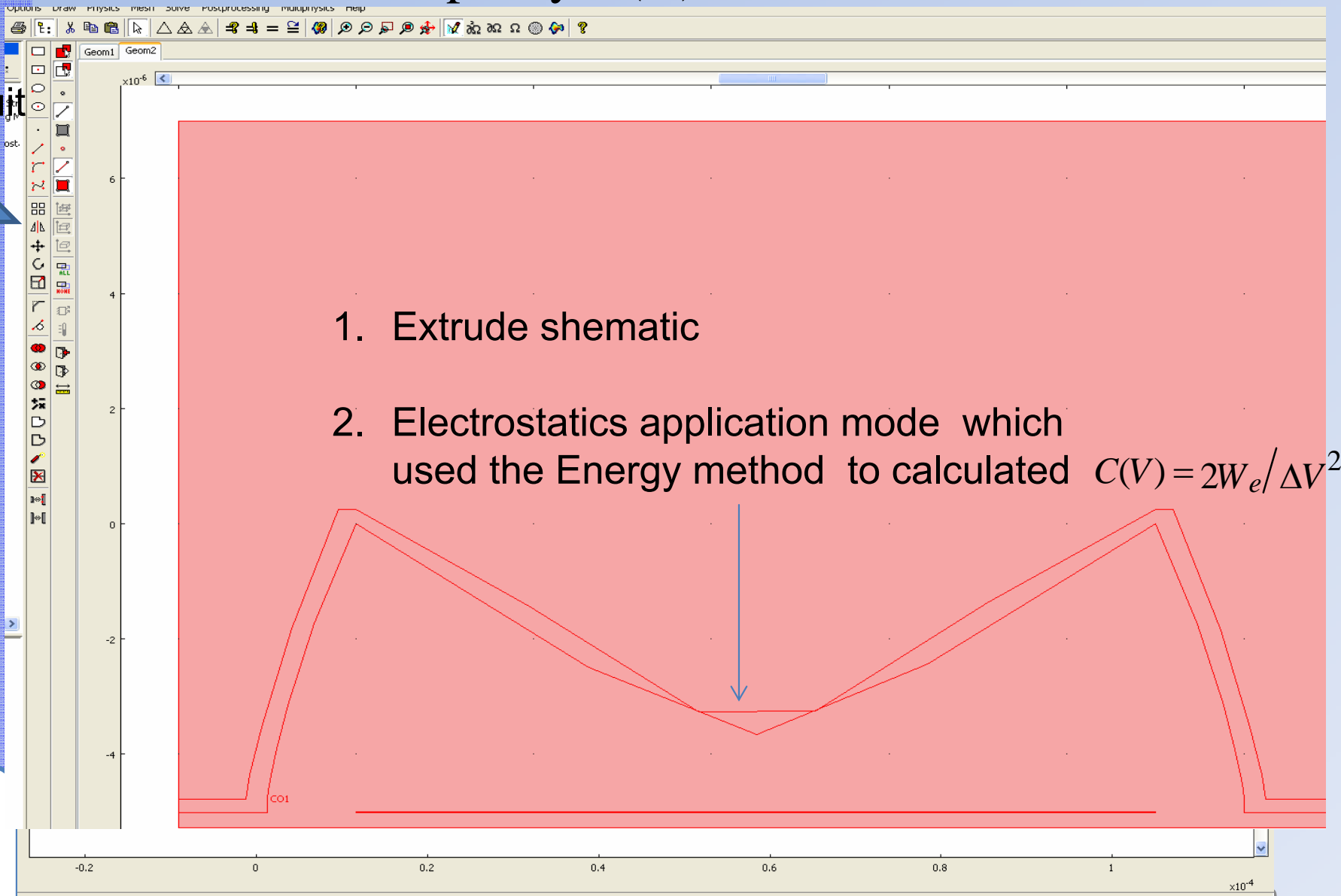
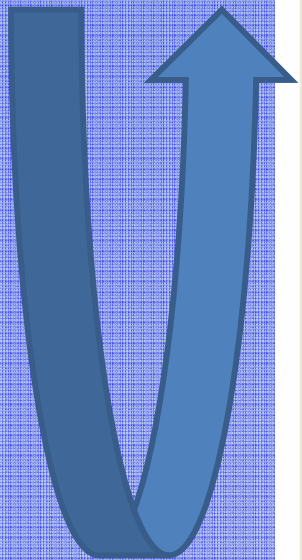
Voltage  $V=60$



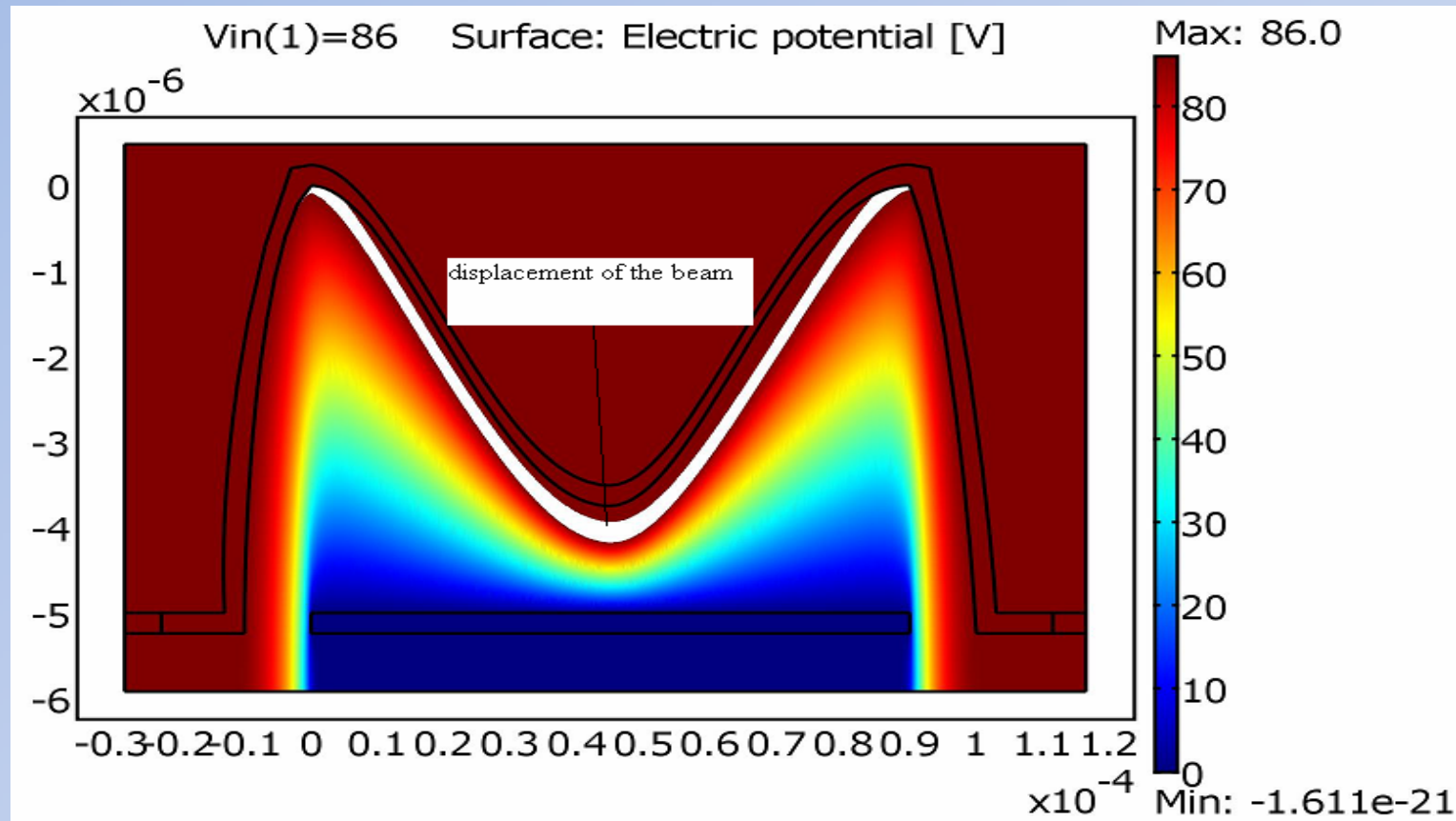
# Comsol Multiphysique beam simulation

## Calculate the capacity $C(V)$

Closed-circuit

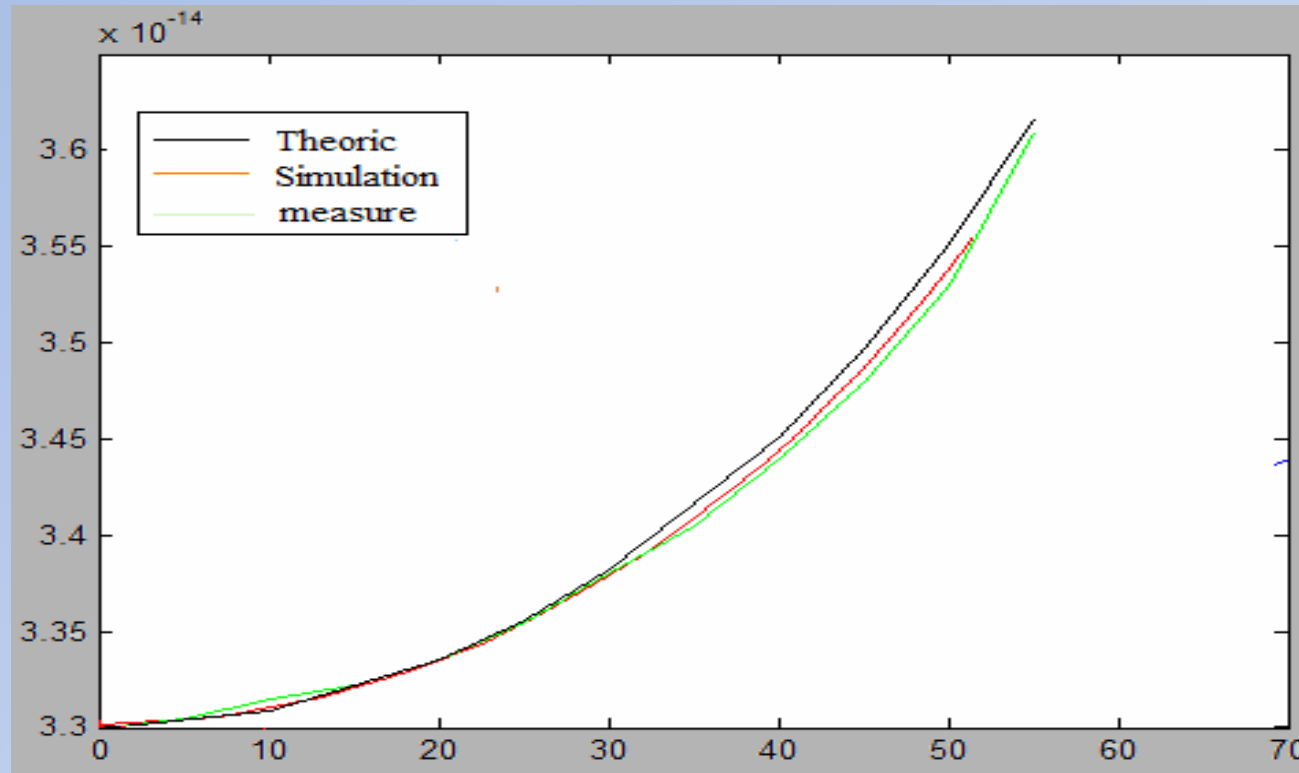


# Comsol Multiphysique beam simulation



**Surface Electric potential, the white color represents the displacement  $y$  after the coupling Electrostatics-Mechanics**

# Comsol Multiphysique beam simulation



**Curves of the comparison between :  
(Theoric, Simulation and measures)**



# Outline

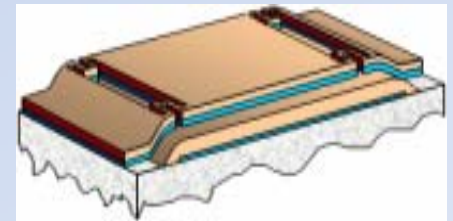
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# Conclusion and Outlook

- ✓ Expression of  $C(V)$  from simple electro-mechanical model, validated by simulation and measures
- ✓ Edge effect is neglected
- ✓ Problem :  $\Delta C/C$  maxi is lowered by the buckling
- ✓ Confirm this model by profilometry measures
- ✓ Refine this model with 3D simulations (COMSOL)
- ✓ Use of these Nb MEMS in millimetrics : superconducting modeling
- ✓ New MEMS device with meandering (2)



(2) Mathias Schicke and Karl.F.Schuster, *IEEE Transactions on Applied Superconducting* , vol.3, No.2, june 2003.

**THANK YOU**