



WIR SCHAFFEN WISSEN – HEUTE FÜR MORGEN

Paul Scherrer Institut

Multiphysics Simulations for the design of a Superconducting magnet for proton therapy

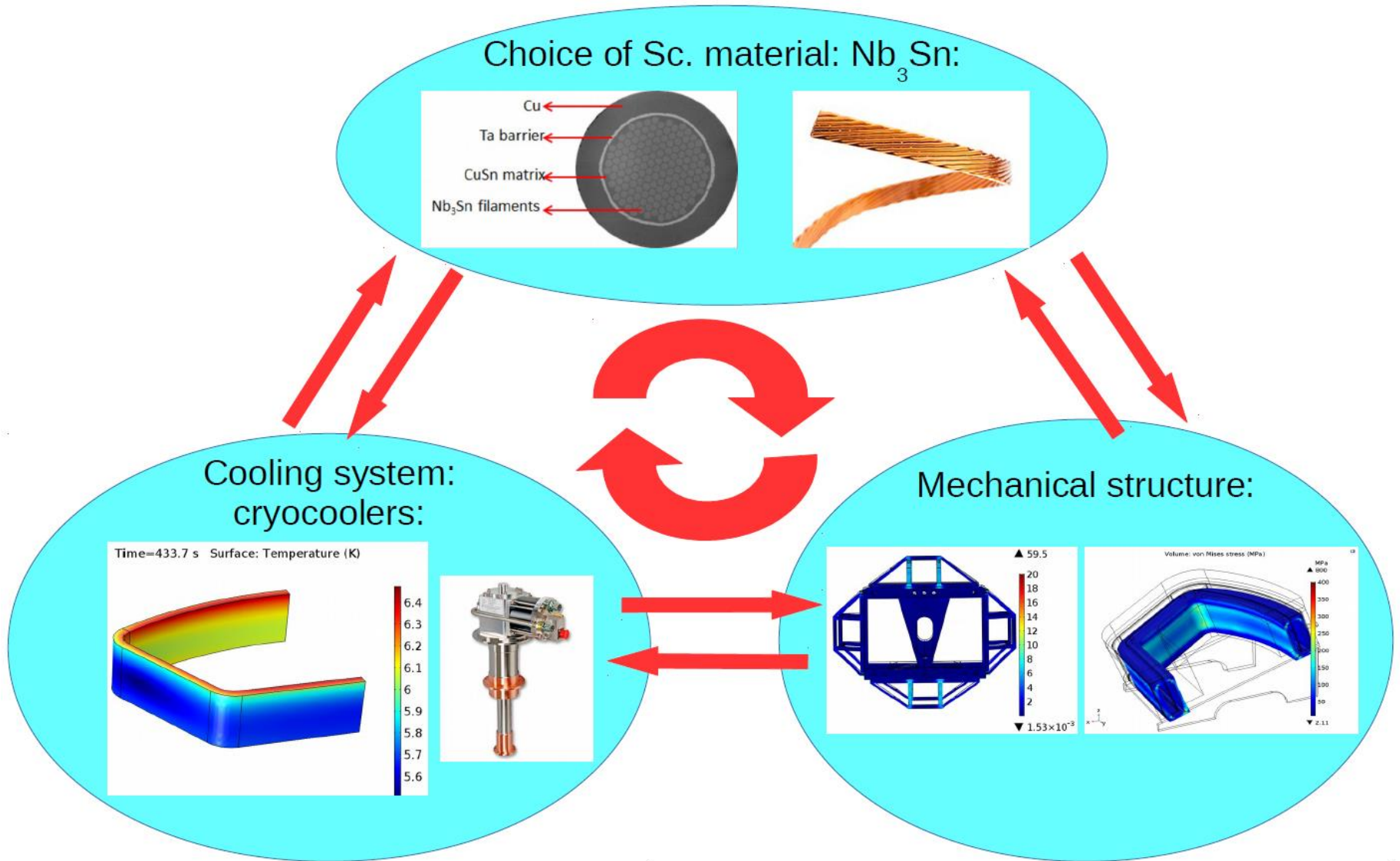
Ciro Calzolaio

October 19, 2017

OUTLINE

- ✓ Superconducting magnets: a Multiphysics approach
- ✓ CAD drawing;
- ✓ Cool-down analysis;
- ✓ Operation
 - ✓ AC losses calculation;
 - ✓ Mechanical analysis.
- ✓ Further steps: Quench analysis

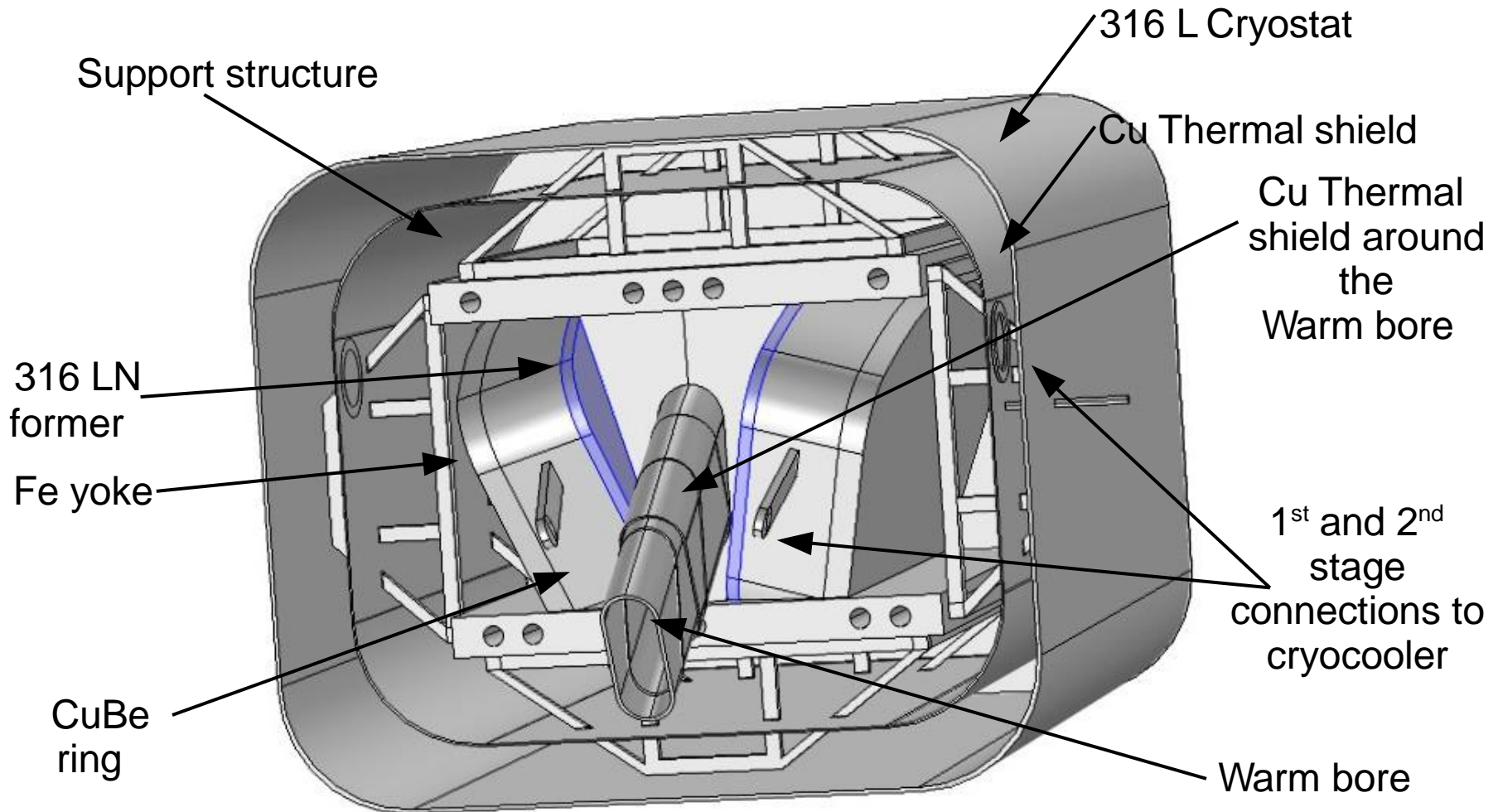
Superconducting magnets: a Multiphysics approach





CAD drawings

Support structure



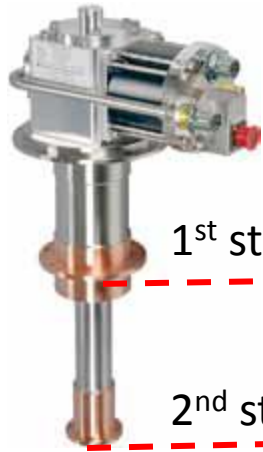
Fully parametric CAD used during the optimization phase.



Cool-down

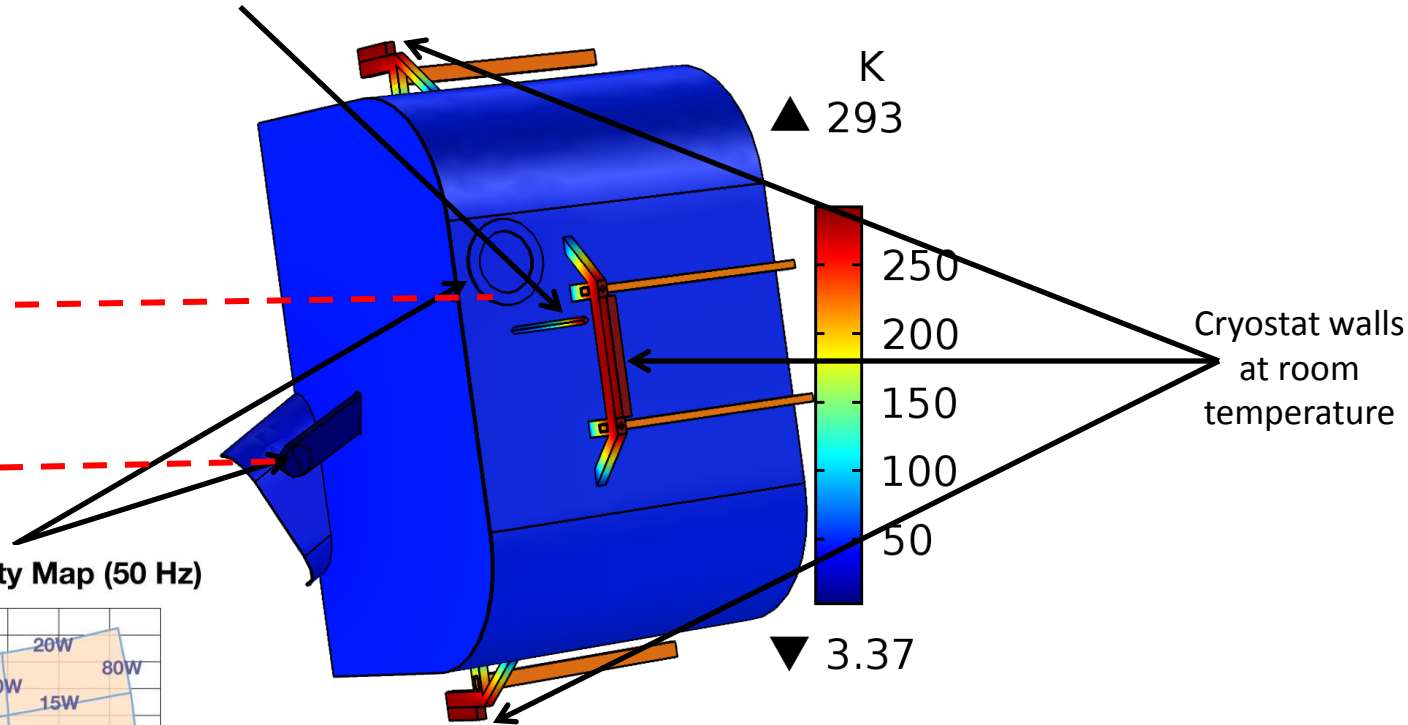
Cool-down

Current lead top
at room temperature

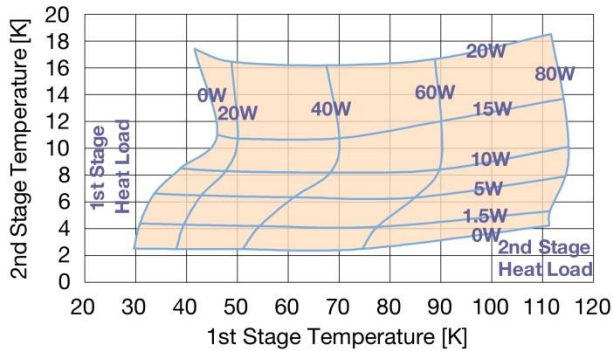


1st stage

2nd stage

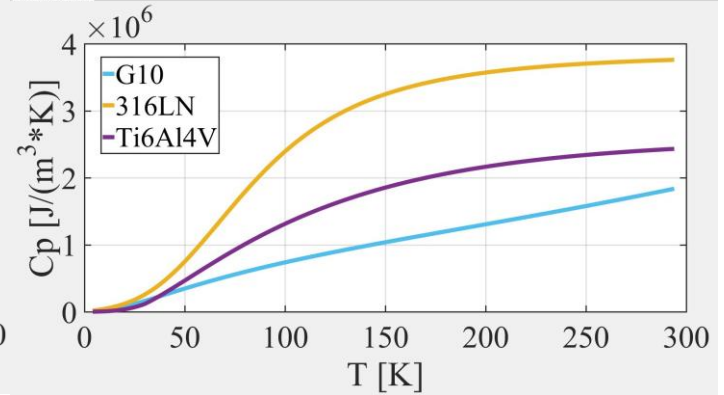
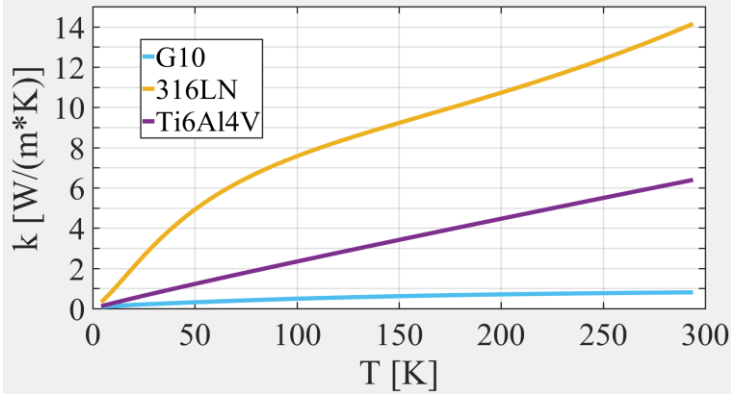
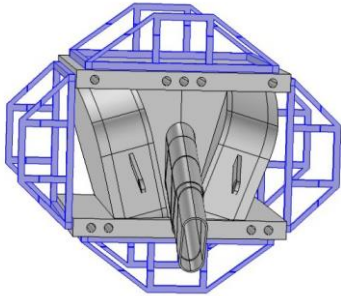


Cryocooler capacity map
SRDK-415D Cold Head Capacity Map (50 Hz)



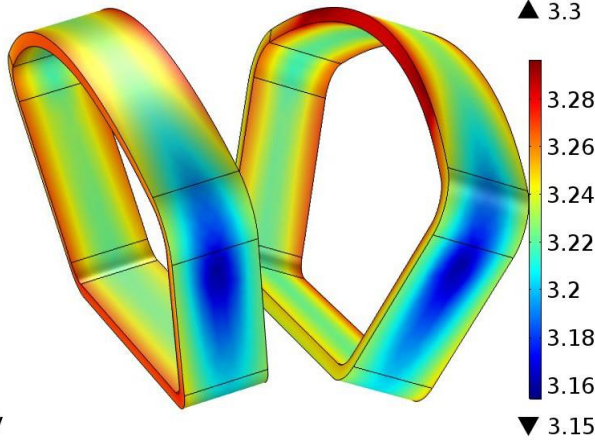
Capacity map implemented as
two arguments interpolating
function.

Support structure: materials choice



G10

Surface: Temperature (K)



Mechanic

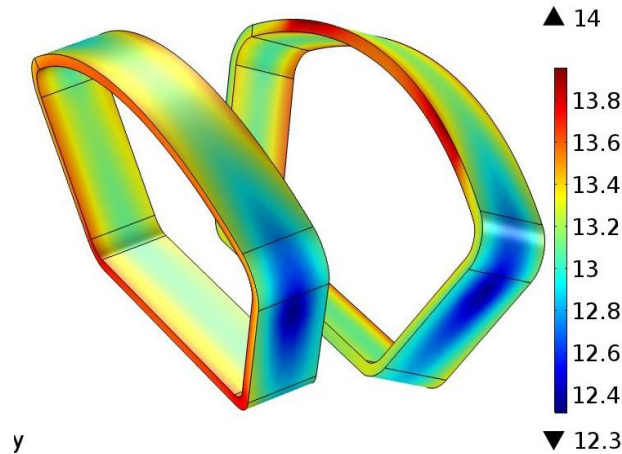


thermal



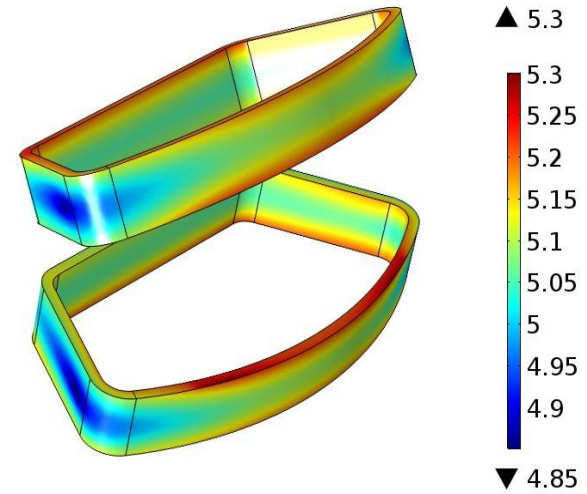
316LN

Surface: Temperature (K)



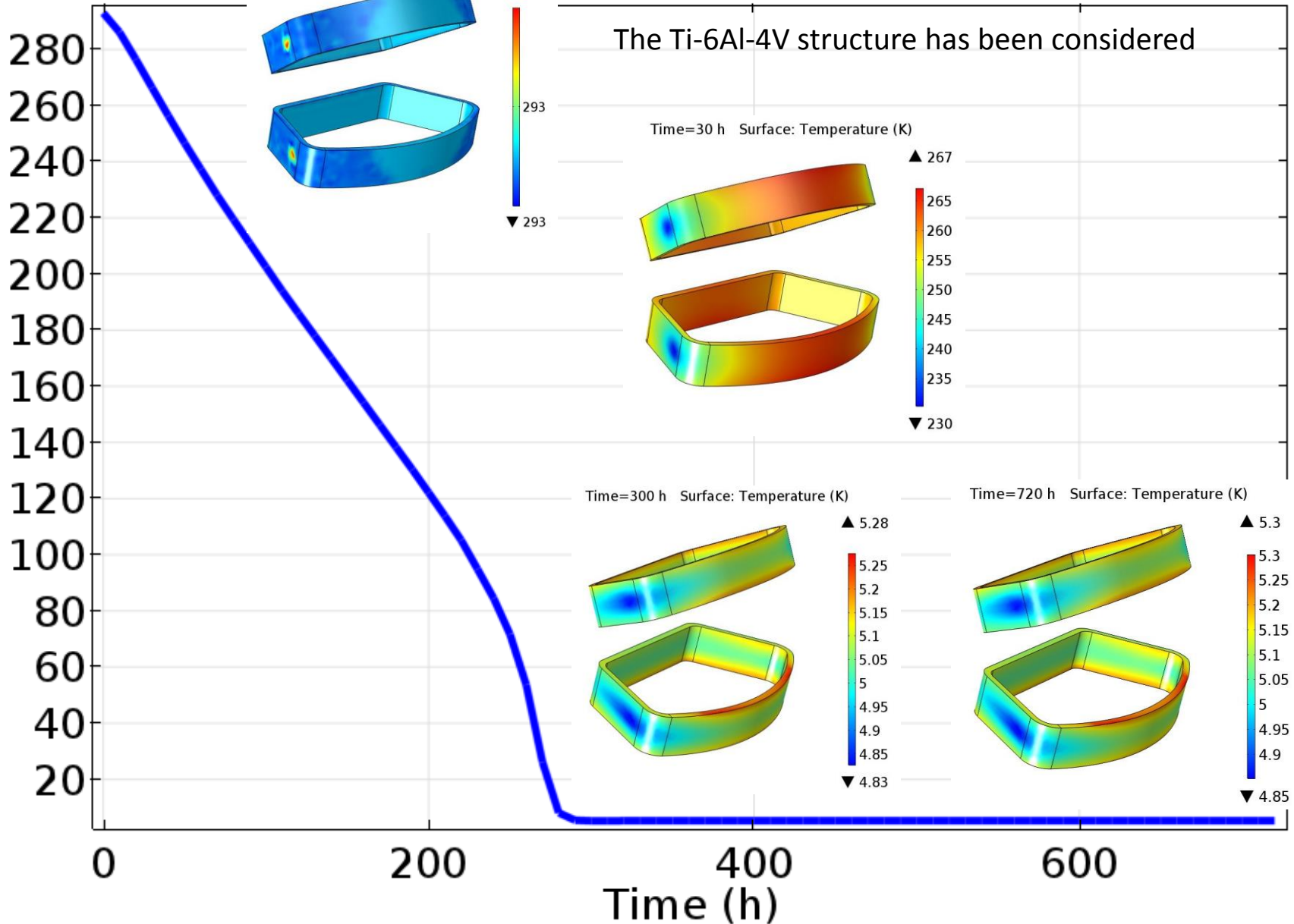
Ti-6Al-4V

Surface: Temperature (K)



Thermal Analysis: cool-down

Temperature (K)

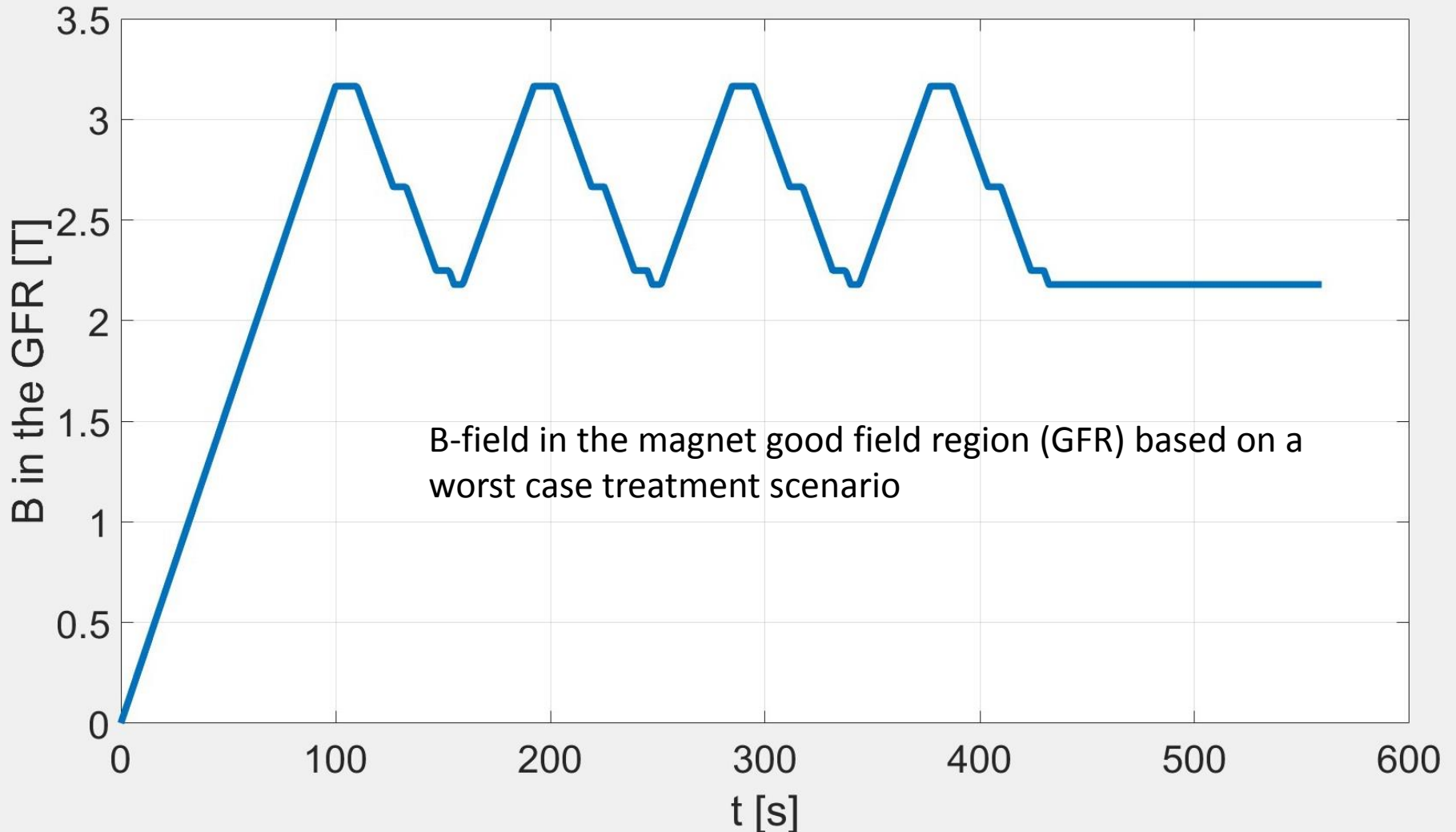




Operation AC-losses

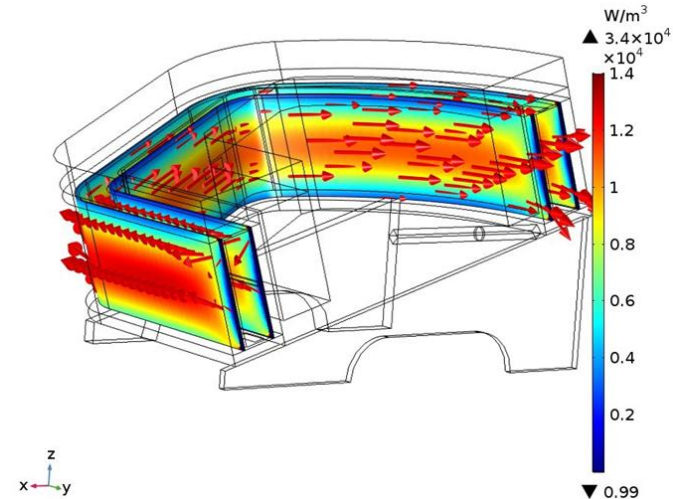
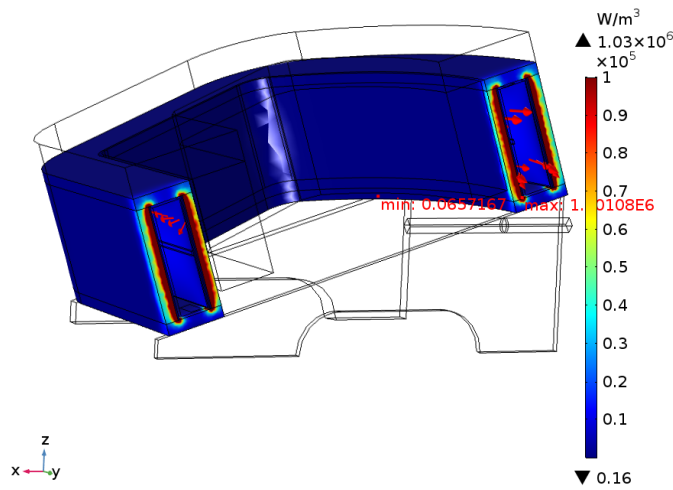
AC losses

To change the protons penetration depth it is necessary to change their energy → the bending field has to change accordingly.



316Ln coil structure: eddy currents

AC losses in the structure

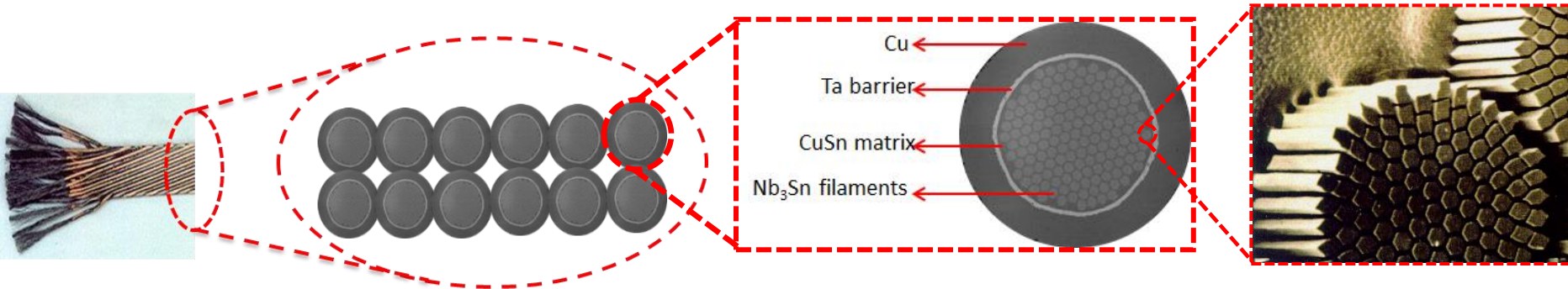


AC losses in the coils

Cable: 4.9 mm x 1.5 mm x 1100 m

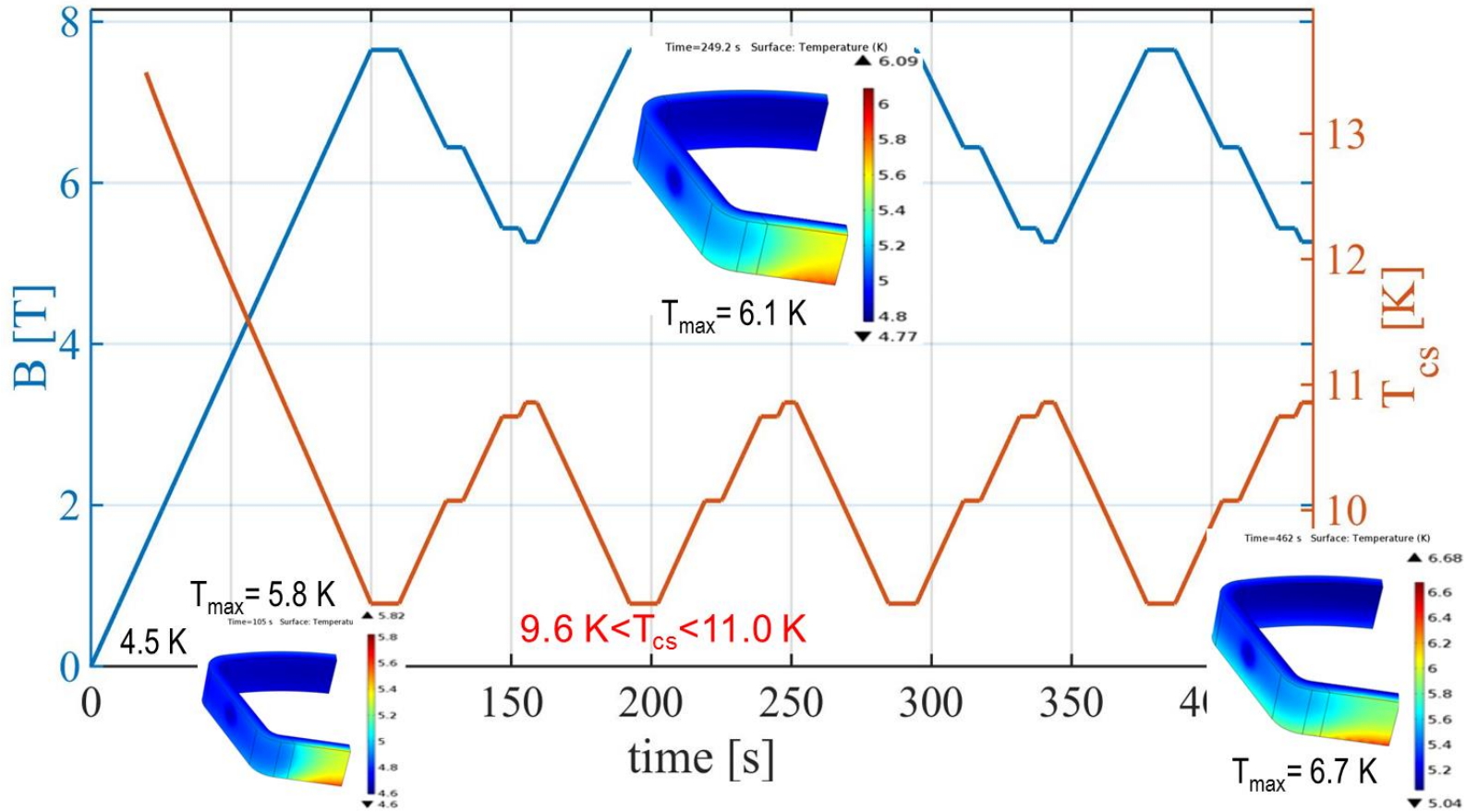
Strand: $\phi = 0.82$ mm

Nb₃Sn Filaments:
 $\phi \sim 4\text{-}5$ μm

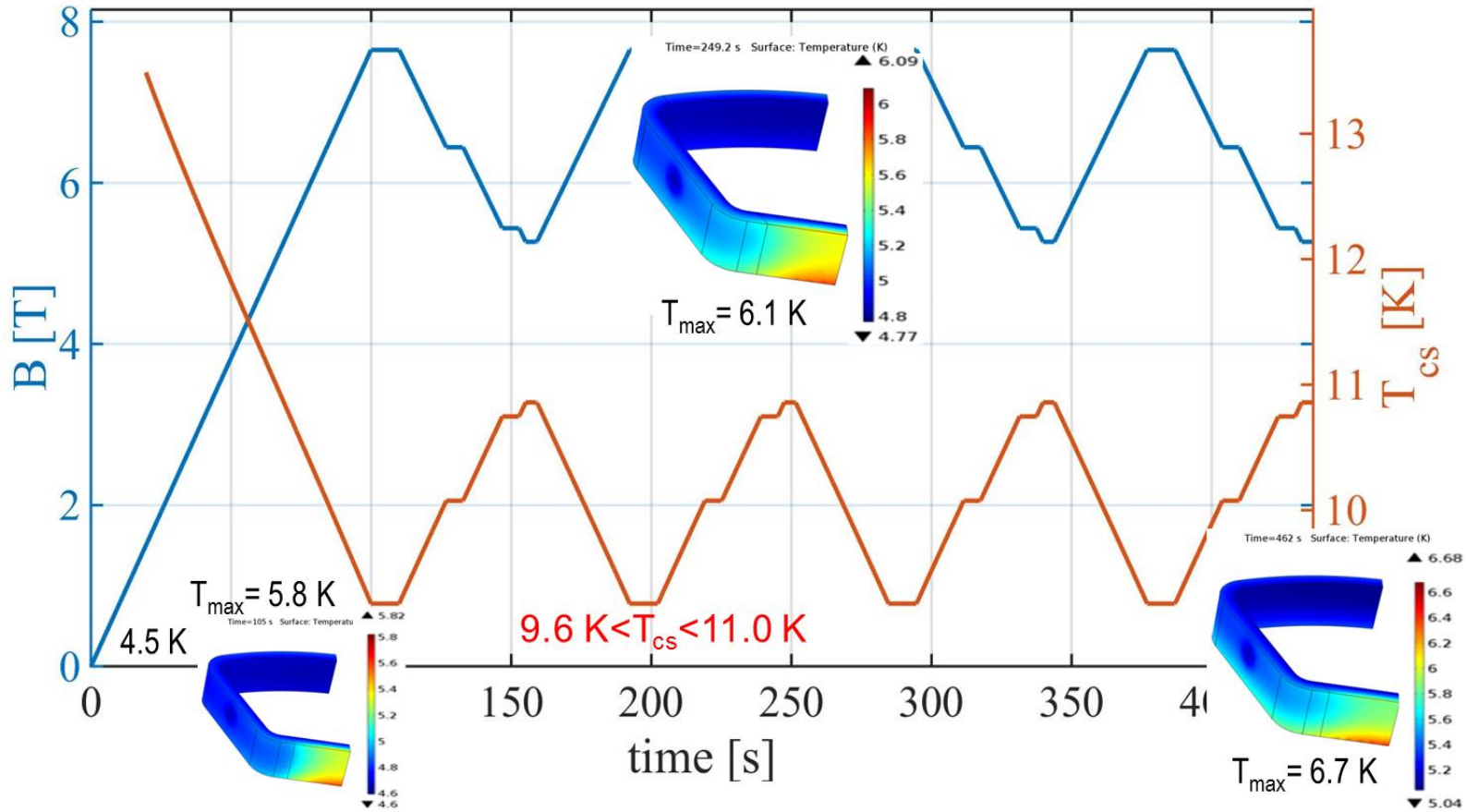


AC losses in the coils (inter-strands + inter-filaments + hysteresis) evaluated analytically

AC losses

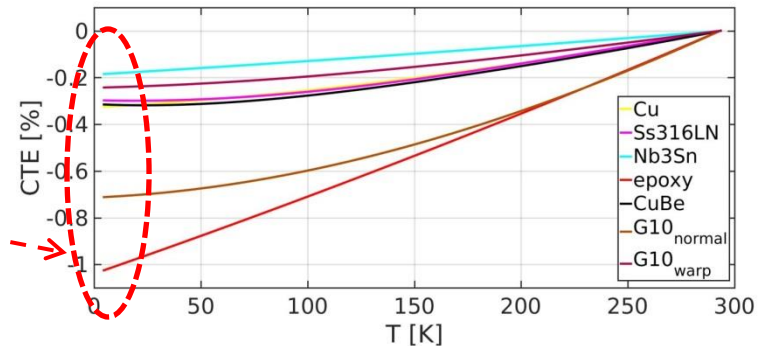


AC losses



It is important to prove that the coils temperature stays below T_{cs} (current sharing temperature) to avoid Joule heating.

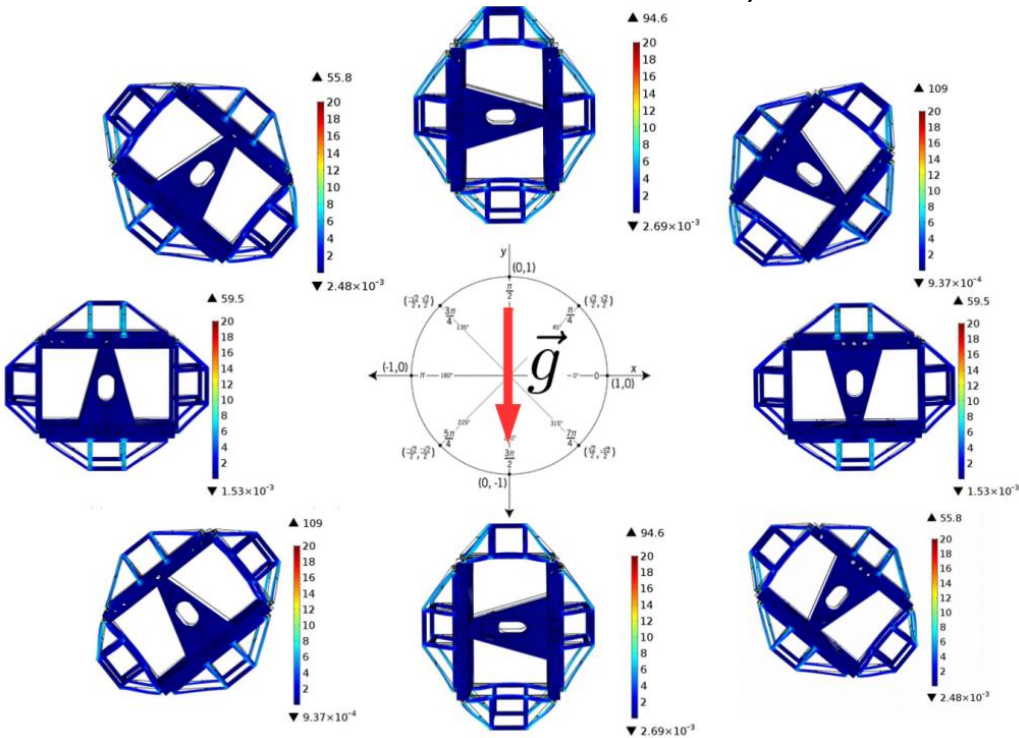
In operation the $\Delta \epsilon_{thermal}$ is negligible





Operation mechanics

1) $\sigma_{Mises} < 110 \text{ MPa}$ upon rotation $< \sigma_{yield}$

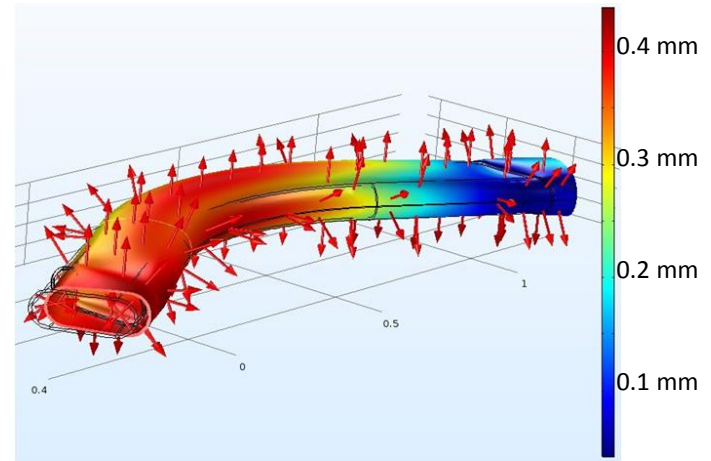


Support structure cryostat verification

1) $\sigma_{Mises} < 110 \text{ MPa}$ upon rotation $< \sigma_{yield}$

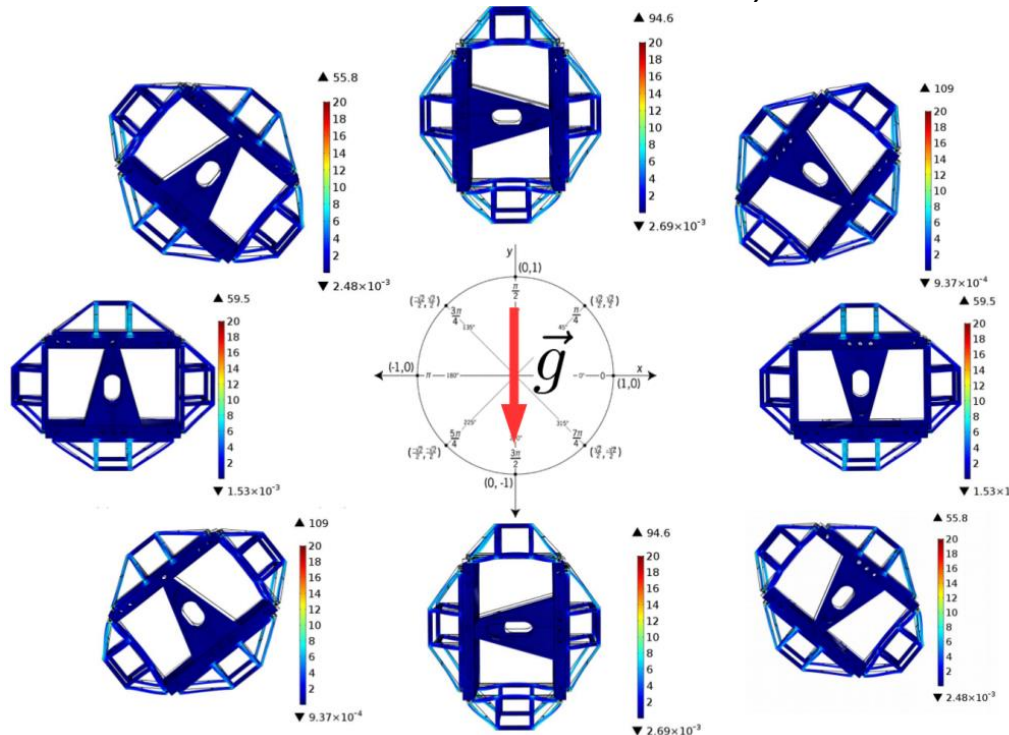
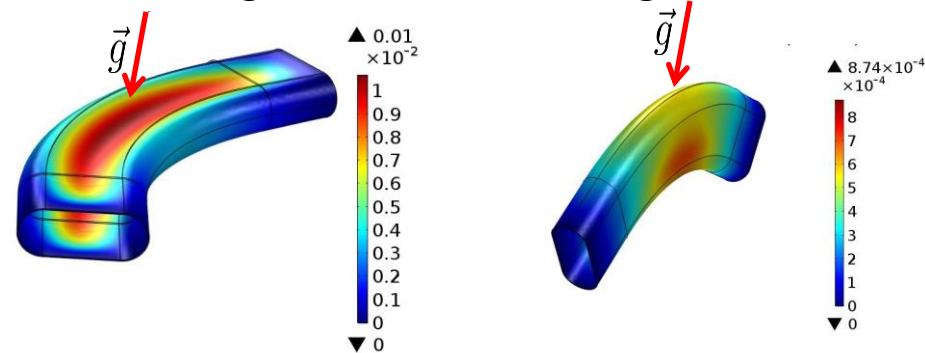
2) Warm bore

- ✓ load $<$ critical load \rightarrow no buckling
- ✓ total displacement $<$ clearances in CAD drawing \rightarrow no thermal bridges



3) Thermal shield

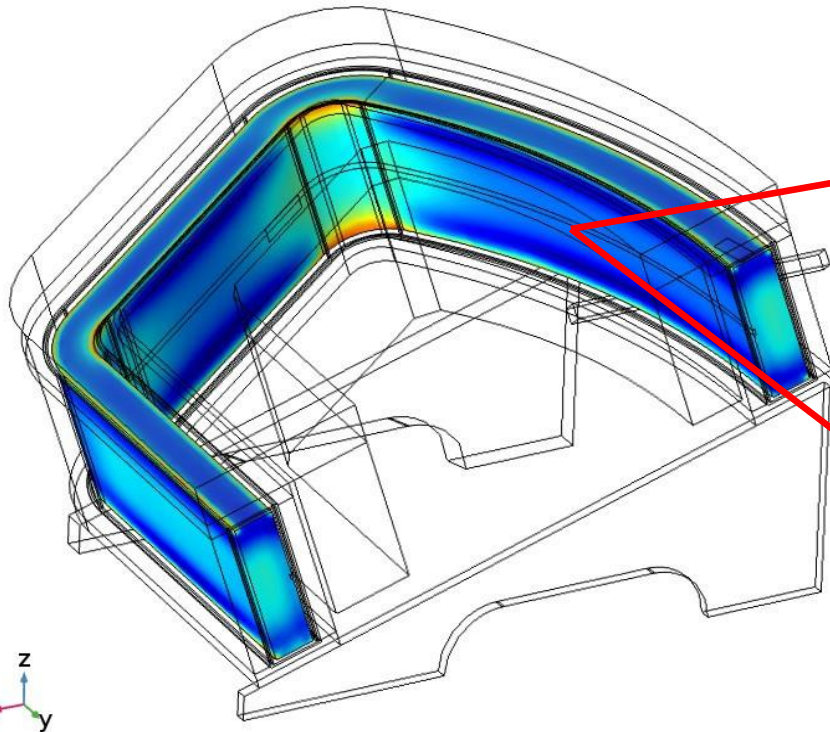
- ✓ total displacement $<$ clearances in CAD drawing \rightarrow no thermal bridges



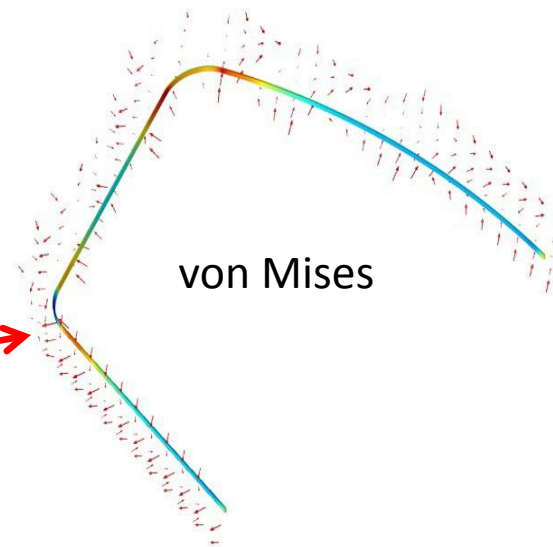
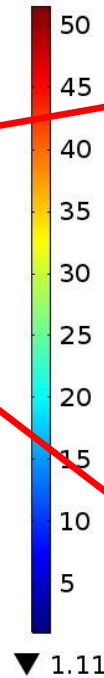
Stress on the conductor

Nb₃Sn is brittle + strain sensitive → it is crucial to monitor the stress/strain the cable
 Lorentz forces + thermal strain were considered.

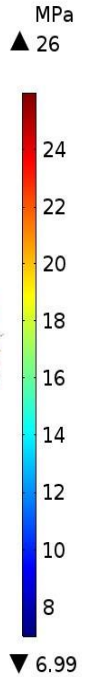
Volume: von Mises stress (MPa)



MPa
▲ 51.6

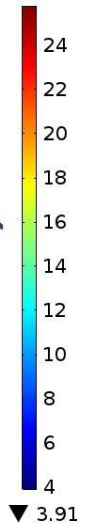


von Mises



MPa
▲ 25.8

Max shear
on cable
insulation



A moderate performance degradation is expected

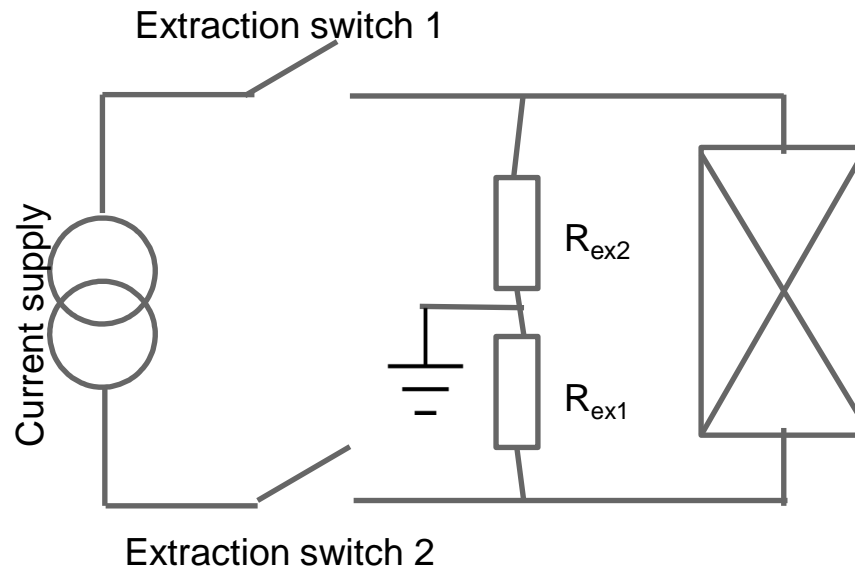


Further steps: Quench analysis

Quench scenario

Despite the efforts during the design phase, a perturbation in the coils may trigger a transition from the superconducting to the normal state, namely a quench.

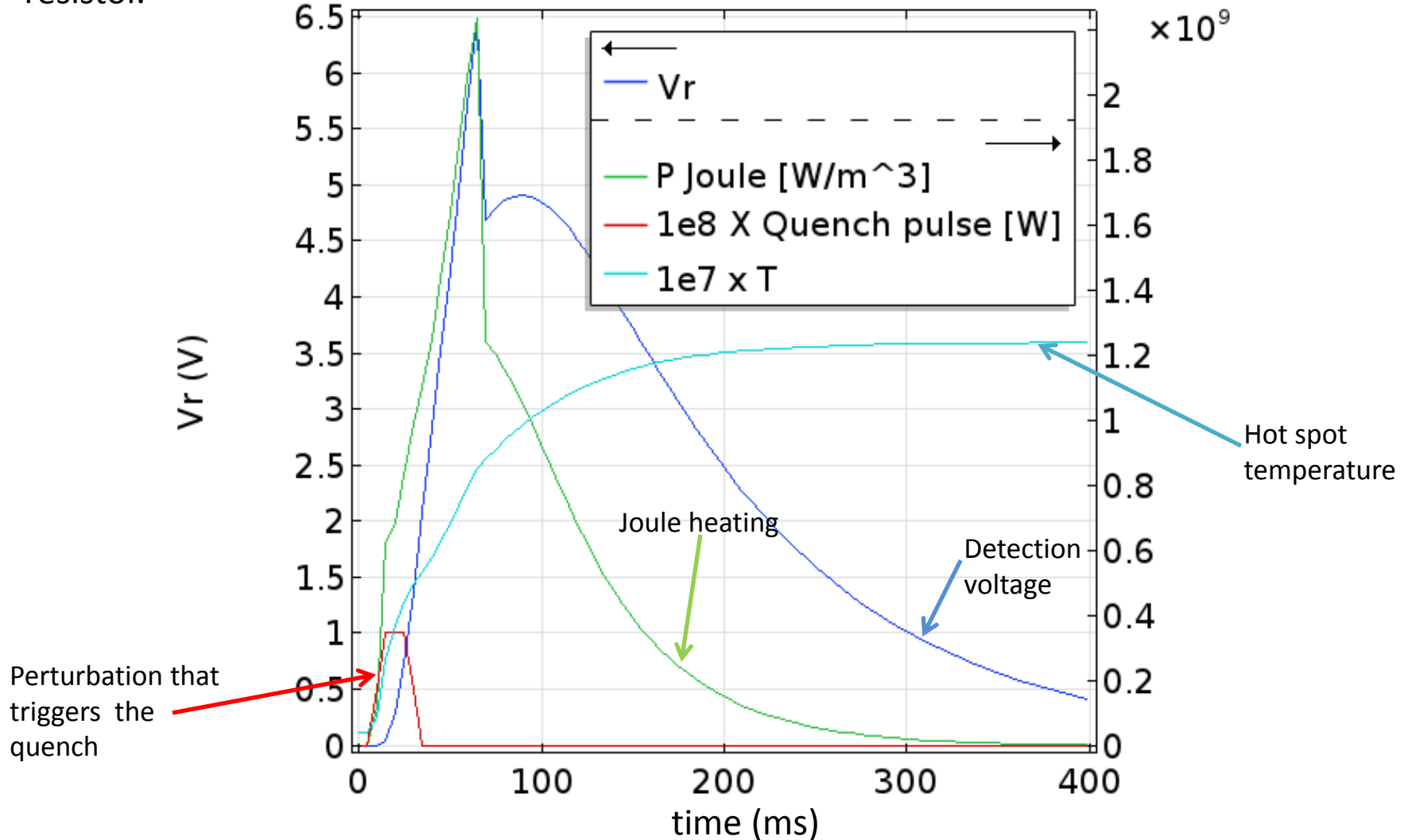
In this case it is necessary to extract the magnet energy and to dump it into an external resistor.



Quench scenario

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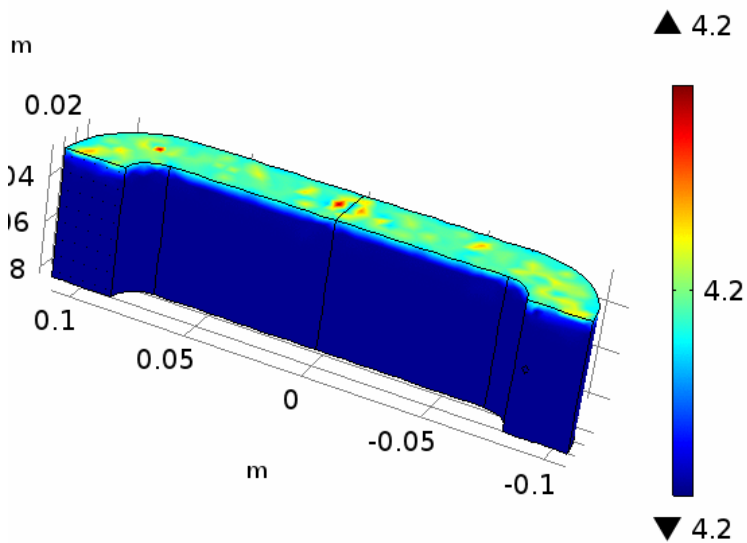


Quench scenario

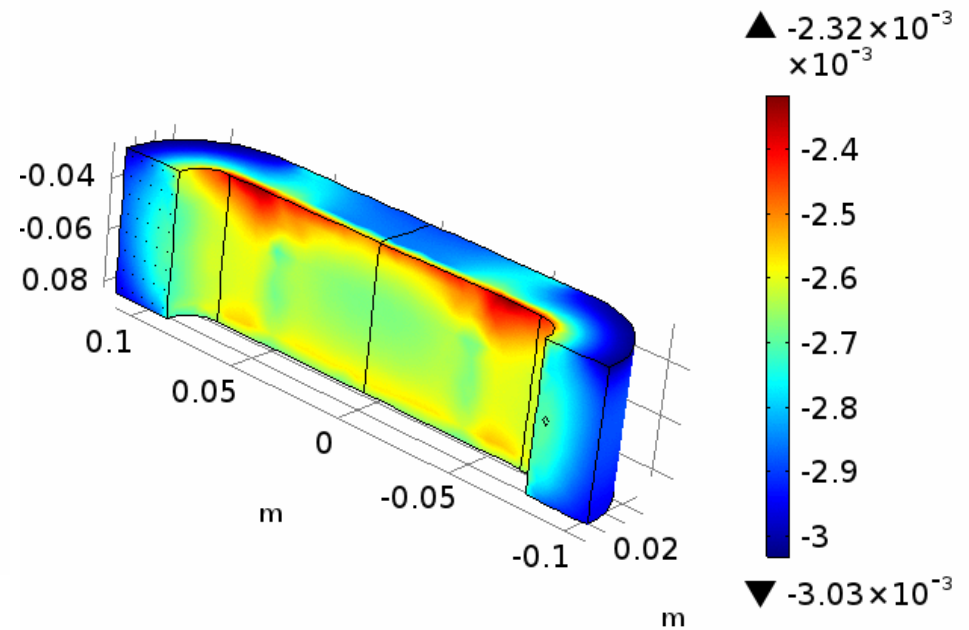
Despite the efforts during the design phase, a perturbation in the coils may trigger a transition from the superconducting to the normal state, namely a quench.

In this case it is necessary to extract the magnet energy and to dump it into an external resistor.

Time=0 s Volume: Temperature (K)



t(1)=0 Volume: First principal strain (1)



Summary

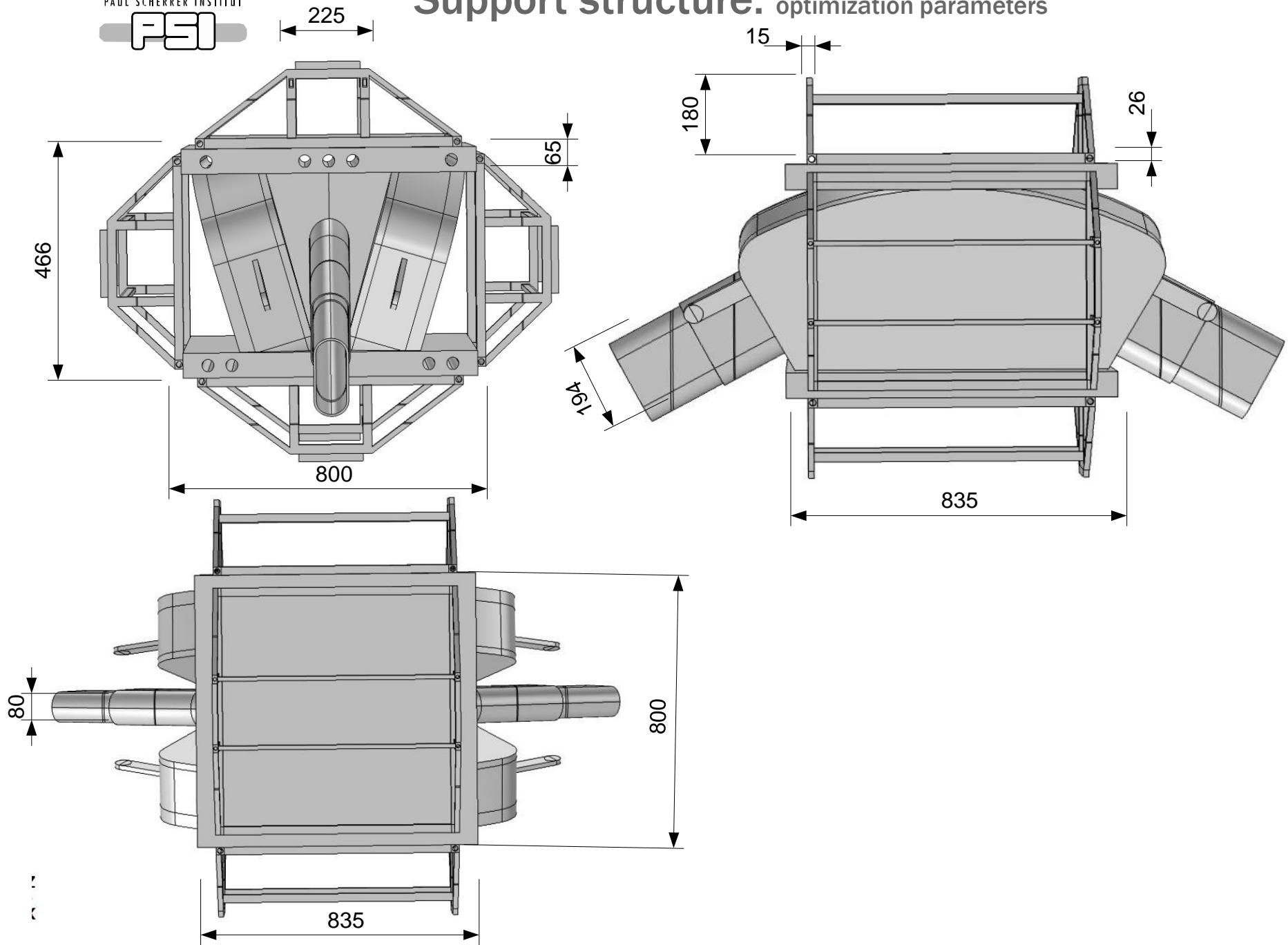
- ✓ Modelling a superconducting coil implies dealing with Multiphysics problems.

- ✓ COMSOL Multiphysics has been used to
 - ✓ Produce a parametric CAD of the magnet;
 - ✓ Analyze the cooldown time and the achievable temperature;
 - ✓ Estimate the AC losses in the magnet in operation;
 - ✓ Check the stress in the structure and in the coils due to the Lorentz forces and the thermal strain;

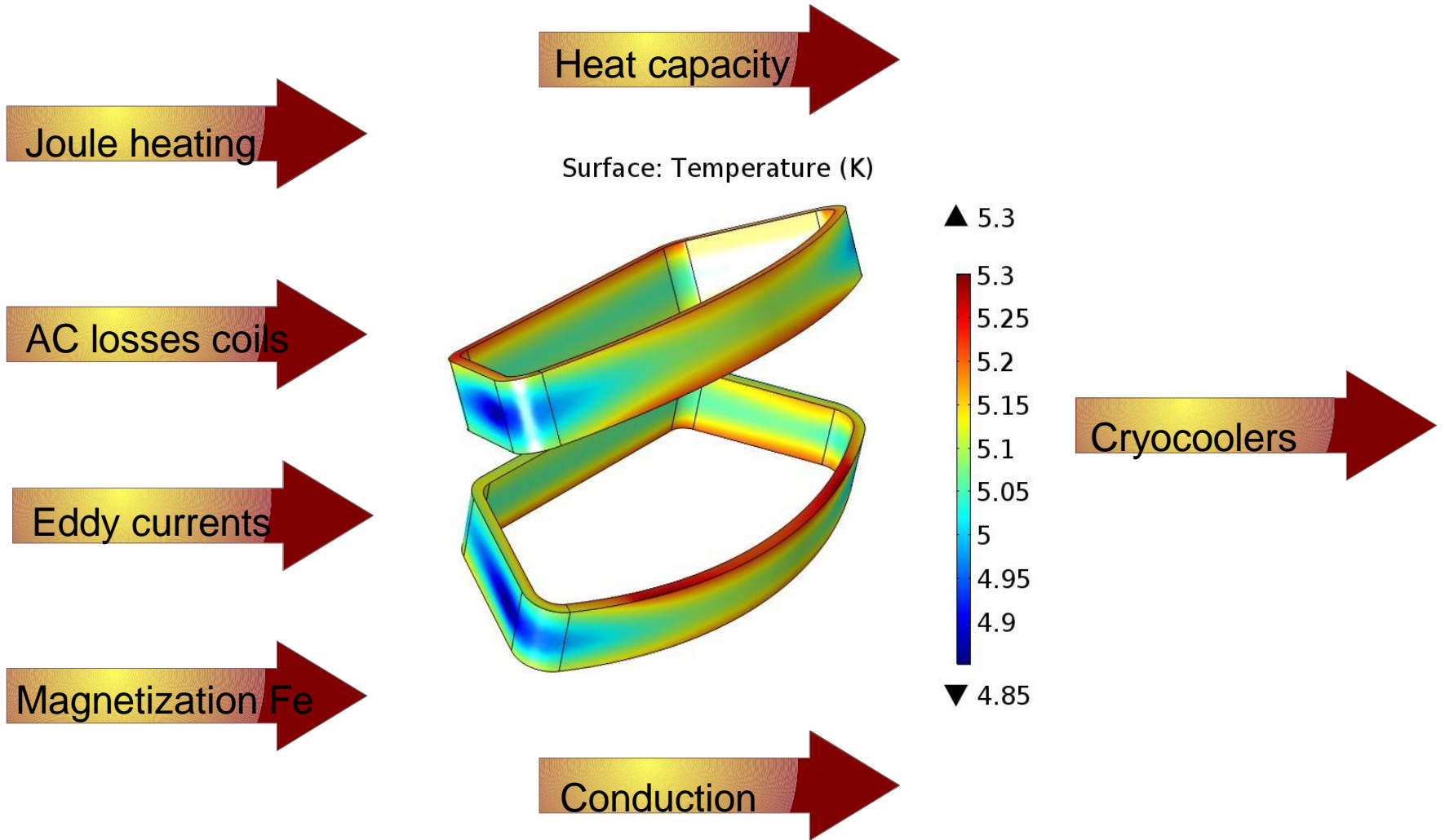
- ✓ In operation it is possible to have perturbations that leads to a quench of the superconducting magnet. In this case
 - ✓ A fast heating of the coils takes place;
 - ✓ If the energy is not safely extracted, the fast heating may even destroy the coils.

APPENDIX

Support structure: optimization parameters



Thermal Analysis



AC losses in the structure

$$\left\{ \begin{array}{l} J = \nabla \times \mathcal{H} \\ B = \nabla \times \mathcal{A} \\ E = -\frac{\partial \mathcal{A}}{\partial t} \\ J = \sigma E + J_e \end{array} \right. \Rightarrow \nabla \times \nabla \times \mathcal{A} = \mu_0 \sigma \frac{\partial \mathcal{A}}{\partial t}$$

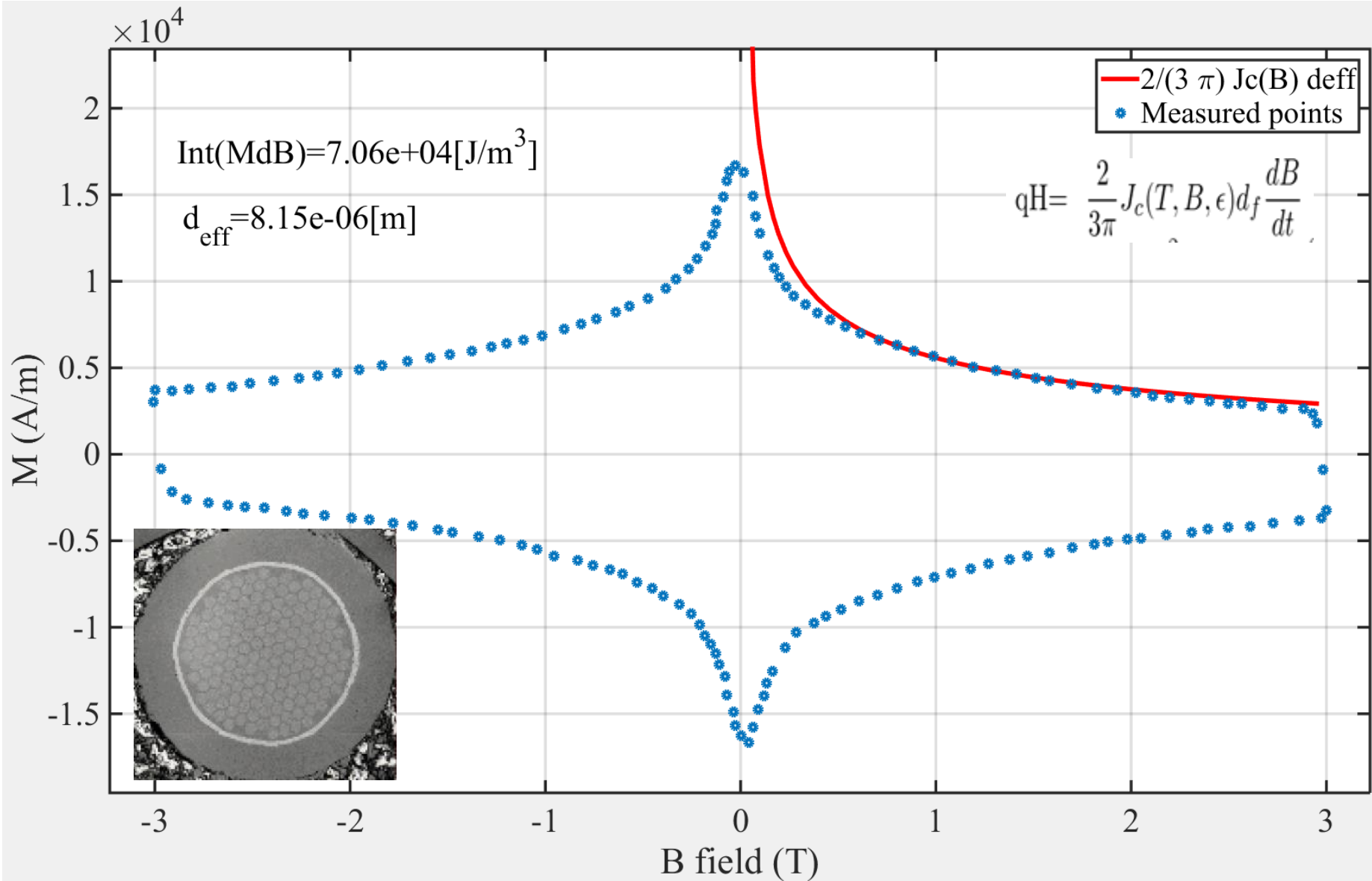
AC losses in the coils

$$\begin{aligned} q_H &= \frac{2}{3\pi} J_c(T, B, \epsilon) d_f \frac{dB}{dt} \\ q_{iF} &= \frac{2}{\mu_0} \left(\frac{dB}{dt} \right)^2 \frac{\mu_0}{2\rho_t} \left(\frac{tp_f}{2\pi} \right)^2 \\ q_{iS} &= \frac{1}{6} \left(\frac{dB}{dt} \right)^2 \frac{1}{R_a} tp_s \frac{c}{b} + \frac{1}{120} \left(\frac{dB}{dt} \right)^2 \frac{1}{R_c} \frac{c}{b} tp_s N_s (N_s - 1) \end{aligned}$$

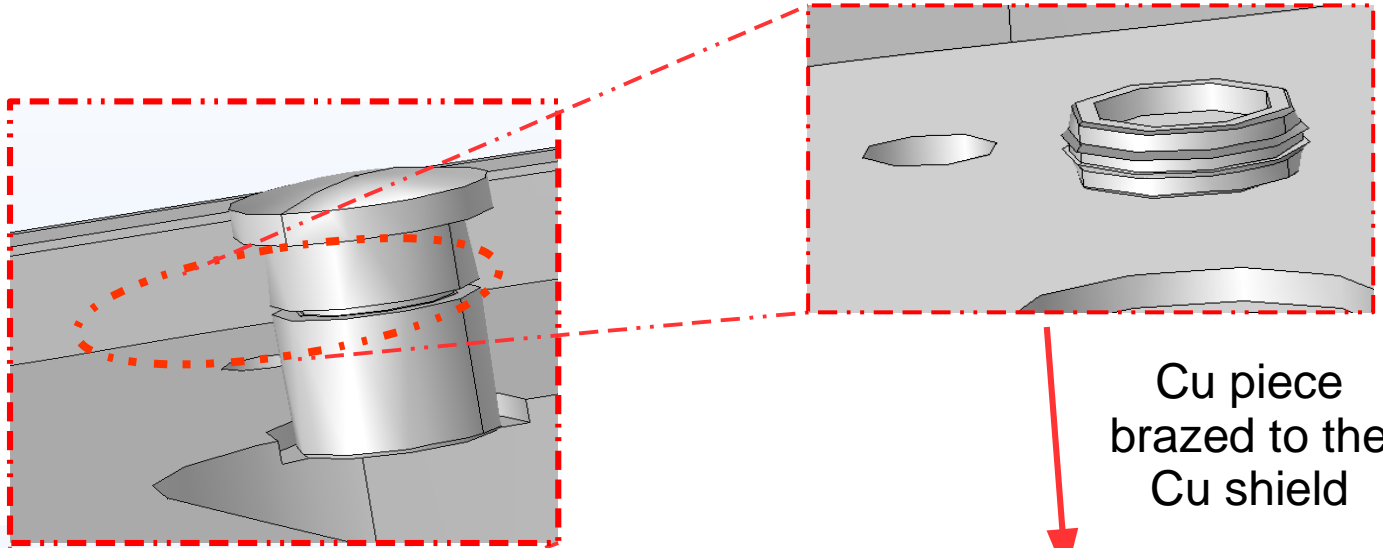
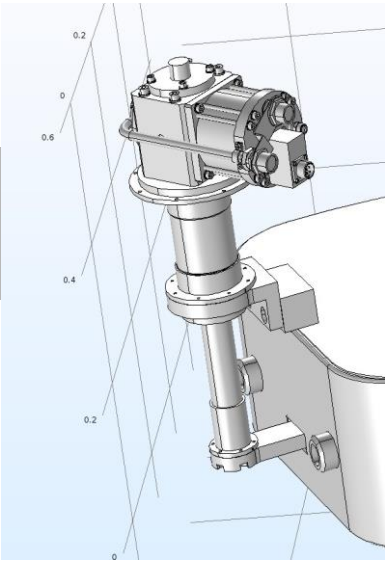
Temperature profile

$$\rho C_p \frac{\partial T}{\partial t} + \nabla \cdot (-k \nabla T) = \rho_{el} J^2 + q_H + q_{iF} + q_{iS}$$

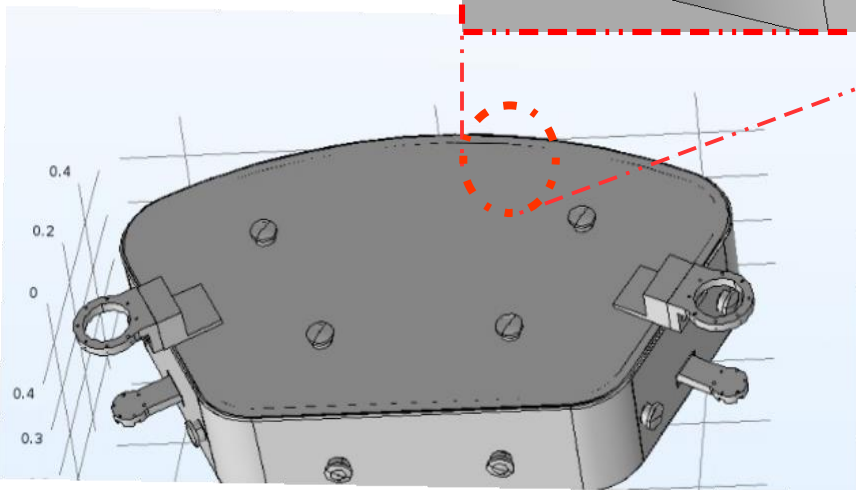
AC losses - hysteresis



DQS structure: 1st stage thermal shield



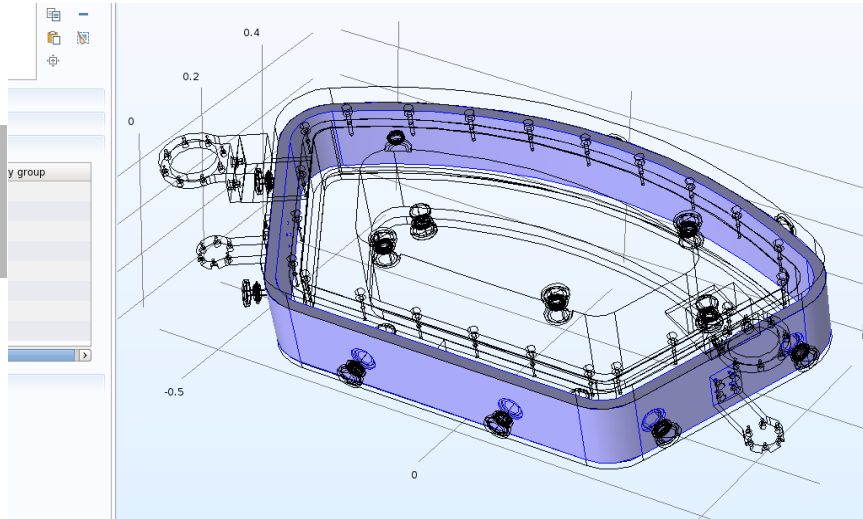
Cu piece
brazed to the
Cu shield



Cu thermal
shield

G10 hollow
pillar

DQS structure



Cu support around the coil.

316 L former

Fe yoke

